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A STUDY ON THE SCALE EFFECTS OF PROPULSIVE CHARACTERISTICS OF PODDED PROPULSORS

SR-2006-18

Stephen Lane

August 2006

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LIST OF ABBREVIATIONS

D	Diameter (Propeller)
DAS	Data Acquisition System
deg	Degree(s)
EAR	Expanded Area Ratio
Hz	Hertz
ITTC	International Towing tank Conference
IOT	Institute for Ocean Technology
J	Advance Coefficient
K _Q	Torque Coefficient
K _T	Thrust Coefficient
m	Metre(s)
mm	Millimetre(s)
m/s(ec)	Metres per Second
n	Shaft Rotational Speed
NRC	National Research Council Canada
NSERC	Natural Sciences and Engineering Research Council of Canada
MUN	Memorial University of Newfoundland
P/D	Pitch-Diameter Ratio
Q	Torque
R _n	Reynolds Number
RPS	Revolutions per Second
Т	Thrust
V	Speed (of advance)
η	Open Water Efficiency
ν	Kinematic Viscosity
ρ	Density (water)

1.0 INTRODUCTION

Podded propellers were introduced to the marine industry just over a decade ago and have since become a popular main propulsion system for ships. This is due to their better hydrodynamic characteristics than conventional propeller-rudder systems.

A podded propeller consists of a motor inside of a pod and a propeller(s) connected to the drive shaft at one or both end(s) of the shaft. The unit is connected to the vessel via a strut, which allows the whole system to rotate 360 degrees around the vertical, or z-axis. This allows for the thrust to be directed anywhere in a 360 degree compass, which gives far superior manoeuvring capabilities. The rapid adoption of podded propellers by the industry has outpaced the understanding of their performance. This lack of knowledge has translated into problems in practice, including propeller and bearing damage as well as vibration during manoeuvring.

The purpose of this study is to increase the understanding of podded propeller performance. NRC could also use these tests as a solid base on which further testing could be completed.

2.0 DESCRIPTION OF THE MUN-NRC-NSERC POD MODEL

The experiments conducted were on either a single podded propeller or two podded propellers operating simultaneously. Two of the cases used a propeller of 270mm diameter, while the remainder used a propeller of 200mm diameter. The arrangement and diameter of propellers are given in the section *DESCRIPTION OF CASES* for each particular case. All cases used a propeller that was four bladed, had a pitch-diameter ratio (P/D) of 1.0, and an expanded area ration (EAR) of 0.6. The geometric particulars of the pod are given below in *Table 1*. The values for the model propulsor were selected to provide an average representation of in-service, full-scale single screw podded propulsor. The geometric particulars of the pod-strut model were defined using the parameters depicted in *Figure 1*.¹

Experimental Dimensions of Model Pods	Pod mm
Propeller Diameter, D _{Prop}	270 or 200
Pod Diameter, D _{Pod}	139
Pod Length, L _{Pod}	410
Strut Height, S _{Height}	300
Strut Chord Length	225
Strut Distance, S _{Dist}	100
Strut Width	60
Fore Taper Length	85
Fore Taper Angle	15°
Aft Taper Length	110
Aft Taper Angle	25°

Table 1: Geometric particulars of the pod-strut model

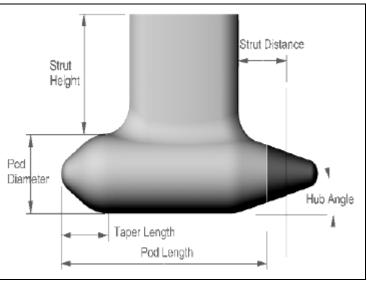


Figure 1: Geometric Parameters

3.0 DESCRIPTION OF FACILITIES

Several of the test cases took place at the NRC-IOT Ice Tank, while one of the test cases studied took place at the MUN Towing Tank. The flowing sub-sections describe the two Tanks that the tests were performed in.

3.1 NRC-IOT Ice Tank

The NRC-IOT ice tank is 90m long, 12m wide and 3m deep. The ice tank is equipped with a towing carriage that is capable of velocities from 0.1 - 4.0m/s. The control room is thermally insulated and houses the computer equipment for the drive control and the instrumentation racks for the model test transducers. The tank can accommodate models from 2-12m in length; and is equipped with force measurement, strain gauge load cells, model motions, accelerometer arrays, along with other instrumentation; all of which allow for various types of tests to be completed in the tank.²

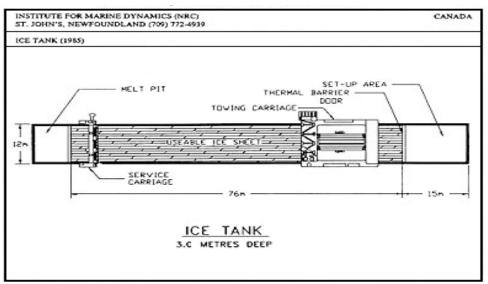


Figure 2: NRC-IOT Ice Tank schematic

3.2 MUN Towing tank

The towing tank facility at MUN has a length of 58m, is 4.5m wide, and a water depth of 2.2m. The tank is equipped with a towing carriage with a maximum towing speed of 5.0m/sec. The tank is equipped with a hydraulically operated wave maker, vertical mesh beaches, precision dynamometer, a 16 channel data acquisition system, along with other instrumentation; all of which allows for various types of testing to be competed at the facility.³

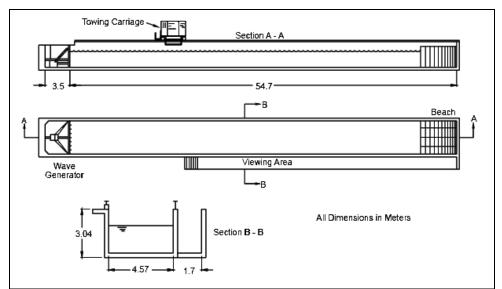


Figure 3: MUN Towing Tank schematic

4.0 DESCRIPTION OF INSTRUMENTATION

4.1 Experimental Apparatus

As in the previous section, this section will also contain a description of the experimental apparatus used at the NRC-IOT Ice Tank as well as the MUN Towing Tank.

4.1.1 NRC-IOT dynamometer

The set-up shown below in *Figure 3* was used for this set of experiments. The system has the ability to measure the propeller and pods forces and moments. It was used to measure unit thrust (T_{unit}), propeller thrust at hub end (T_{prop}), propeller thrust at pod end (T_{pod}), propeller torque (Q), as well as forces in the three coordinate directions.³ The unit thrust is of particular interest, as it used for powering predictions for podded propellers. The unit thrust is the net available thrust available for propelling the ship. It not only includes the thrust of the propeller, but also the drag and other hydrodynamic forces acting on the podstrut body.

The design includes an instrumented propeller hub, a custom mitre gearbox, an azimuth drive system, propeller drive system, a hull mounting and seal assembly, and a 6-component balance for measuring global loads on the pod.⁴

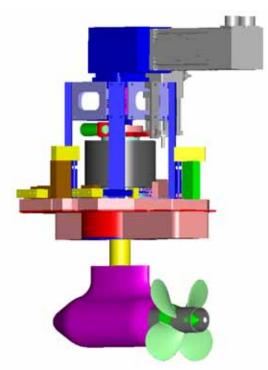


Figure 4: TDC Podded Props – General Arrangement



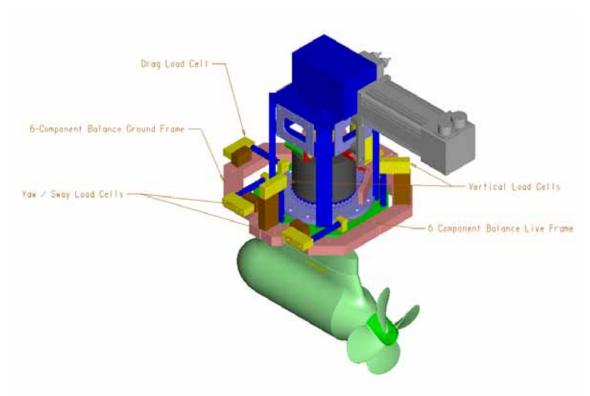


Figure 5: 6-Component Balance

4.1.2 NSERC-NRC pod dynamometer (or MUN dynamometer)

The NSERC-NRC pod dynamometer system, custom designed, was used during the experiments. The system has the ability to measure the propeller and pods forces and moments. It was used to measure unit thrust (T_{unit}) , propeller thrust at hub end (T_{prop}) , propeller thrust at pod end (T_{pod}) , propeller torque (Q), as well as forces in the three coordinate directions.³ The unit thrust is of particular interest, as it used for powering predictions for podded propellers. The unit thrust is the net available thrust available for propelling the ship. It not only includes the thrust of the propeller, but also the drag and other hydrodynamic forces acting on the pod-strut body. The water temperature, carriage speed (V), and the rotational speed of the propeller (n) were also measured.

As can be seen below in Figure 3, the unit consists of two major components. The first part is the pod dynamometer, which measures the thrust and torque of the propeller at the propeller shaft. The second part of the unit is the global dynamometer, which measures the unit forces in the three coordinate directions at a location above the propeller boat. Also, a boat shaped body called a wave shroud was attached to the frame of the test equipment and placed just above the water surface. Further details of the experimental apparatus can be found in MacNeill et al. (2004).⁵



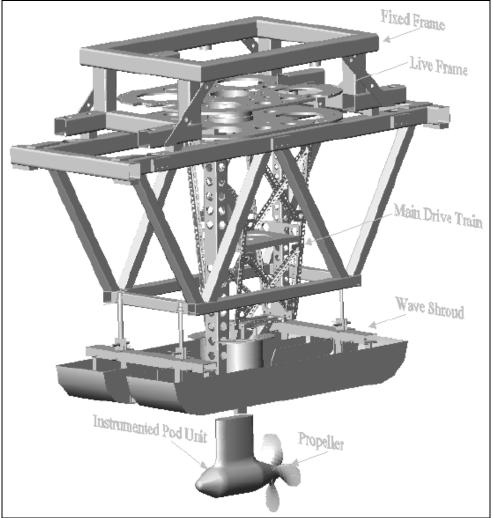


Figure 6: NSERC-NRC Pod Dynamometer System



Figure 7: Global dynamometer looking from below



Figure 8: Side view of system

4.2 **Opens Boat**

For the experiments conducted in the NRC-IOT Ice Tank an opens boat was constructed out of plywood, foam and glass. The opens boat floor was provided with slots that the pod drives fit into to allow the distance between the drives to be varied from as close as the drives could safely be run together to 3 times the width spacing of the pods.⁴

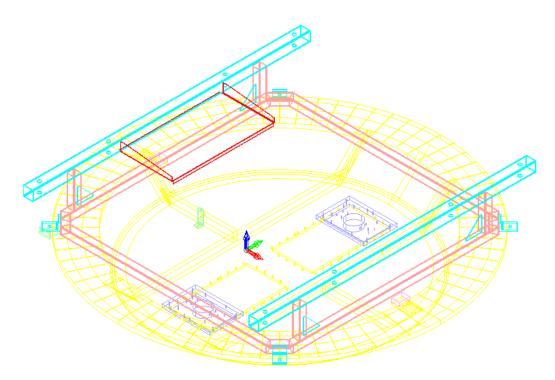


Figure 9: Round Opens Boat

4.3 Data Acquisition System (DAS)

4.3.1 NRC-IOT tests

The Data Acquisition System (DAS) for this project is custom built with IOTech gear and RS232 data from the U500 controller. The system components were chosen to allow for the system to be placed into a free running model. The data was collected through a total of 26 channels; a detailed outline of the channel set-up is in *Appendix C*. The system consisted of the following:

- 1 Panasonic CF-51 Laptop, PC4026, S/N
- 1 Panasonic Docking Station
- 1 D-Link DI-624 Wireless Router
- 1 IOTech Daqbook 2001, S/N 802671
- 2 IOTech DBK 43A, 8 Channel Stain Gage Modules
- 1 Custom 16 Channel DBK 43A to 10 Pin breakout box
- 2 IOTech DBK 45, 4-Channel SSH and Low-Pass Filter Cards
- 1 IOTech DBK 10, Expansion Chassis
- 1 Custom 8-Channel Isolation Amp box



Figure 10: DAS set-up used for calibrations

4.3.2 MUN tests

The data for each of the test conditions was collected through 13 channels (three channels for propeller and pod thrusts and torque, two channels for shell drag, six channels for global loads, one channel for propeller rotational speed and one channel for carriage speed). The voltage data outputs for the tests were collected using an IOTech Daqbook data acquisition system (Daqbook 2000) connected to a computer running DaqView software. For these tests, the data were collected with a sampling rate of 59Hz. The raw data was collected in .txt format and post processed using Microsoft Excel. For each test run, data was collected for at least 10 second when the propeller run at very low rps (0.5 or less). Then the test data was collected following a standard procedure. The data collected at low rps was used to tare the test value. In this way the friction correction for thrust and torque was avoided.

5.0 DESCRIPTION OF CASES

As stated above, there were a total of seven sets of tests conducted. This section is intended to give a brief explanation of each case and the tests that were performed for each set of tests. A general test plan will be provided in each sub-section for each case.

5.1 Case 1

The tests were performed in the MUN Towing Tank in January 2005. The experiments conducted were on a single podded propeller with a diameter of 270mm. The following is a list of the types of experiments conducted: Reynolds Number Effects Tests, Air Friction and Bollard Runs, Opens Tests (0 deg azimuth), Oblique Flow Tests, and Third Quadrant Runs.

Reynolds Number Effects	
Mode	Pull Mode
RPS	8 , 9 , 10, 11, 12 , 13, 14
Carriage Velocity (m/s)	1.728, 1.944, 2.16, 1.944, 2.187, 2.43, 2.16, 2.43, 2.7, 2.376, 2.673, 2.97, 2.592, 2.916, 3.24, 2.808, 3.159, 3.51, 3.024, 3.402, 3.78
Azimuth Angle (deg)	0

Table 2: General test plan	for Reynolds Effects Tests
----------------------------	----------------------------

Air Friction Tests	
Mode	Pull Mode
RPS	1,2 (in both positive and negative directions)
Carriage Velocity (m/s)	0
Azimuth Angle (deg)	0

Table 3: General test plan for Air Friction Tests

Bollard Runs	
Mode	Pull Mode
RPS	-11 to 10
Carriage Velocity (m/s)	0
Azimuth Angle (deg)	0

Table 4: General test plan for Bollards Tests

Opens Tests	
Mode	Pull Mode
RPS	12
Carriage Velocity (m/s)	0.324, 0.648, 0.972, 1.296, 1.62, 1.944, 2.268, 2.592, 2.916, 3.24, 3.564
Azimuth Angle (deg)	0

Table 5: General test plan for Open Tests

Oblique Flow Tests	
Mode	Pull Mode
RPS	12
Run #1	
Carriage Velocity (m/s)	2.268, 1.62, 0.324, 3.24, 0.648, 0.972, 2.592, 1.944, 3.564, 1.296, 2.916, 4.0
Azimuth Angle (deg)	-9
Run #2	
Carriage Velocity (m/s)	-1.62, -1.296, -0.324, -0.648, -0.972, -1.944
Azimuth Angle (deg)	-9
Run #3	
Carriage Velocity (m/s)	2.268, 1.62, 0.324, 3.24, 0.648, 0.972, 2.592, 1.944, 3.564, 1.296, 2.916, 4.0
Azimuth Angle (deg)	9
Run #4	
Carriage Velocity (m/s)	-1.62, -1.296, -0.972, -1.944, -1.05
Azimuth Angle (deg)	9

Table 6: General test plan for Oblique Flow Tests

Third Quadrant Tests	
Mode	Pull Mode
RPS	12
Carriage Velocity (m/s)	0.324, 0.648, 0.972, 1.296, 1.62, 1.944
Azimuth Angle (deg)	0

Table 7: General test pan for Third Quadrant Tests

5.2 Case 2

This is the numerical results of the same set-up as case 1; and was completed on Oct 24/04. They were computed for a single podded propeller with a 270mm diameter. Mohammed Islam and Dr. Pengfei Liu completed the test using the program PROPELLA.

5.3 Case 3

Tests were conducted in the NRC-IOT Ice Tank in March of 2006 on a single podded propeller of 200mm diameter. The following is a list of the types of experiments performed: Reynolds Number Effect Tests, Air Friction and Bollard Runs, and Open Tests.

Pull Mode
0
0.01. 0.1, 1, 14, 15
0
0.01. 0.1, 1, 14, 15
0
0.01, 0.1, 1, 7, 10, 13, 14, 15
0

Table 8: General test plan for Air Friction Tests

Bollard Runs	
Mode	Pull Mode
Carriage Velocity (m/s)	0
Run #1	
RPS	0.01, 0.1, 1, 14, 15
Azimuth Angle (deg)	0
Run #2	
RPS	0.01, 0.1, 1, 14, 15
Azimuth Angle	0
Run #3	
RPS	0.01, 0.1, 1, 7, 10, 13, 14, 15
Azimuth Angle	0

Table 9: General test plan for Bollard Runs

Opens Tests		
Mode	Pull Mode	
Run #1		
Carriage Velocity (m/s)	0.66, 2.64, 3.30, 3.63, 3.96	
RPS	16.5	
Azimuth Angle (deg)	0	
Run #2		
Carriage Velocity (m/s)	0.60, 2.40, 3.00, 3.30, 3.60	
RPS	15	
Azimuth Angle (deg)	0	
Run #3		
Carriage Velocity (m/s)	0.52, 2.08, 2.60, 2.86, 3.12	
RPS	13	
Azimuth Angle (deg)	0	
Run #4		
Carriage Velocity (m/s)	0.40, 1.60, 2.00, 2.20, 2.40	
RPS	10	
Azimuth Angle (deg)	0	
Run #5		
Carriage Velocity (m/s)	0.28, 1.40, 1.68	
RPS	7	
Azimuth Angle (deg)	0	

Table 10: General test plan for Opens Tests

5.4 Case 4 (a and b)

These tests were completed in the NRC-IOT Ice Tank in May of 2006 on a single podded propeller with a diameter of 200mm. For case 4a Pod B was static while for case 4b Pod A was static. The only test completed for this case was Opens Tests at low Froude numbers. This was mainly due to time constraints on the ice tank, and means that comparing the results with the other cases is difficult.

Opens Tests	
Mode	Pull Mode
Run #1	
Carriage Velocity (m/s)	0, 0.13, 0.26, 0.39, 0.52, 0.65, 0.78, 0.91, 1.04
Pod 1	
RPS	0
Azimuth Angle (deg)	0
Pod 2	

RPS	13
Azimuth Angle (deg)	0
Run #2	
Carriage Velocity (m/s)	0, 0.13, 0.26, 0.39, 0.52, 0.65, 0.78, 0.91, 1.04
Pod 1	
RPS	13
Azimuth Angle (deg)	0
Pod 2	
RPS	0
Azimuth Angle (deg)	0

 Table 11: General test plan for Opens Tests

5.5 Case 5 (a and b)

Case 5a and 5b were also completed in the NRC-IOT Ice Tank in May of 2006. The tests were completed on two podded propellers operating simultaneously with a diameter of 200mm. Case 5a is the data collected for Pod A only while case 5b is the data collected for Pod B only. The following is a list of the types of experiments conducted: Air Friction and Bollard Runs, Opens Tests (0 deg azimuth), Oblique Flow Tests, and Dynamic Tests.

Air Friction Tests	
Mode	Pull Mode
Carriage Velocity (m/s)	0
Run #1	
Pod 1	
RPS	0, 0.01, 0.1, 0.2, 0.5, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15
Azimuth Angle (deg)	0
Pod 2	
RPS	0
Azimuth Angle (deg)	0
Run #2	
Pod 1	
RPS	0
Azimuth Angle (deg)	0
Pod 2	
RPS	0, 0.01, 0.1, 0.2, 0.5, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15
Azimuth Angle (deg)	0
Run #4	
Pod 1	
RPS	0

Azimuth Angle (deg)	0
Pod 2	
RPS	0, 0.01, 0.1, 0.2, 0.5, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15
Azimuth Angle (deg)	0

Table 12: General test plan for Air Friction Tests

Bollard Runs	
Mode	Pull Mode
Carriage Velocity (m/s)	0
Run #1	
Pod 1	
RPS	0, 0.01, 0.1, 0.2, 0.5, 1, 2, 3, 4, 5, 11, 12, 13
Azimuth Angle (deg)	0
Pod 2	
RPS	0
Azimuth Angle (deg)	0
Run #2	
Pod 1	
RPS	0
Azimuth Angle (deg)	0
Pod 2	
RPS	0, 0.01, 0.1, 0.2, 0.5, 1, 2, 3, 4, 5, 11, 12, 13
Azimuth Angle (deg)	0
Run #3	
Pod 1	
RPS	0, 0.01, 0.1, 0.2, 0.5, 1, 2, 3, 4, 5, 11, 12, 13
Azimuth Angle (deg)	0
Pod 2	
RPS	0, 0.01, 0.1, 0.2, 0.5, 1, 2, 3, 4, 5, 11, 12, 13
Azimuth Angle (deg)	0

Table 13: General test plan for Bollards Tests

Opens Tests	
Mode	Pull Mode
Run #1	
Carriage Velocity (m/s)	0, 0.13, 0.26, 0.39, 0.52, 0.65, 0.78, 0.91, 1.04, 1.17, 1.3, 1.56, 1.82, 2.08, 2.34, 2.47, 2.6, 2.86, 3.12
Pod 1	

RPS	0, 0.1, 13
Azimuth Angle (deg)	0
Pod 2	
RPS	0, 0.1, 13
Azimuth Angle (deg)	0
T 11 14 G 1	

Table 14: General test plan for Open Tests

Oblique Flow Tests				
Mode	Pull Mode			
Run #1				
Carriage Velocity (m/s)	0, 0.13, 0.26, 0.39, 0.52, 0.65, 0.78, 0.91, 1.04, 1.3, 1.56, 1.82, 2.08, 2.34, 2.47, 2.6, 2.86, 3.12			
Pod 1				
RPS	0, 0.1, 13			
Azimuth Angle (deg)	5			
Pod 2				
RPS	0, 0.1, 13			
Azimuth Angle (deg)	0			
Run #2				
Carriage Velocity (m/s)	0, 0.13, 0.26, 0.39, 0.52, 0.65, 0.78, 0.91, 1.04			
Pod 1				
RPS	0, 0.1, 13			
Azimuth Angle (deg)	10			
Pod 2				
RPS	0, 0.1, 13			
Azimuth Angle (deg)	0			
Run #3				
Carriage Velocity (m/s)	0, 0.13, 0.26, 0.39, 0.52, 0.65, 0.78, 0.91, 1.04			
Pod 1				
RPS	0, 0.1, 13			
Azimuth Angle (deg)	30			
Pod 2				
RPS	0, 0.1, 13			
Azimuth Angle (deg)	0			
Run #4				
Carriage Velocity (m/s)	0, 0.13, 0.26, 0.39, 0.52, 0.65, 0.78, 0.91, 1.04			
Pod 1				
RPS	0, 0.1, 13			
Azimuth Angle (deg)	60			

Pod 2			
RPS	0, 0.1, 13		
Azimuth Angle (deg)	0		
Run #5			
Carriage Velocity (m/s)	0, 0.13, 0.26, 0.39, 0.52, 0.65, 0.78, 0.91, 1.04		
Pod 1			
RPS	0, 0.1, 13		
Azimuth Angle (deg)	60		
Pod 2			
RPS	0, 0.1, 13		
Azimuth Angle (deg)	60		
	60		

Table 15: General test plan for Oblique Flow Tests

Dynamic Tests					
Mode	Pull Mode				
Run#1					
RPS	13				
Carriage Velocity (m/s)	0, 0.13, 0.26, 0.39, 0.52, 0.65, 0.78, 0.91, 1.04, 1.17				
Azimuth Rate	2, 5, 10, 20				
Pod 1					
Azimuth Angle (deg)	5				
Pod 2					
Azimuth Angle (deg)	0				
Run #2					
RPS	13				
Carriage Velocity (m/s)	0, 0.13, 0.26, 0.39, 0.52, 0.65, 0.78, 0.91, 1.04, 1.17				
Azimuth Rate	2, 5, 10, 20				
Pod 1					
Azimuth Angle (deg)	10				
Pod 2					
Azimuth Angle (deg)	0				
Run #3					
RPS	13				
Carriage Velocity (m/s)	0, 0.13, 0.26, 0.39, 0.52, 0.65, 0.78, 0.91, 1.04, 1.17				
Azimuth Rate	2, 5, 10, 20				
Pod 1					
Azimuth Angle (deg)	5				

5			
13			
0, 0.13, 0.26, 0.39, 0.52, 0.65, 0.78, 0.91, 1.04, 1.17			
2, 5, 10, 20			
10			
10			

Table 16: General test plan for Dynamic Tests

5.6 Case 6

This was another numerical simulation of the average pod geometry. They were computed for a single podded propeller with a 200mm diameter. Mohammed Islam and Dr. Pengfei Liu also completed the test using the program PROPELLA.

5.7 Case 7

Tests were conducted in May of 2006 in the NRC-IOT Ice Tank. The tests were conducted on a single podded propeller with a diameter of 200mm. The types of experiments conducted were Air Friction and Bollard Runs, Opens Tests, and Oblique Flow Tests.

Air Friction Tests			
Mode	Pull Mode		
Carriage Velocity (m/s)	0		
Run #1			
RPS	0, 0.01, 0.1, 0.2, 0.5, 1, 2, 3, 4, 5, 11, 12, 13		
Azimuth Angle (deg)	0		
Run #2			
RPS	0, 0.01, 0.1, 0.2, 0.5, 1, 2, 3, 4, 5, 11, 12, 13		
Azimuth Angle (deg)	0		
Run #3			
RPS	0, 0.01, 0.1, 0.2, 0.5, 1, 2, 3, 4, 5, 11, 12, 13		
Azimuth Angle (deg)	0		

Table 17: General test plan for Air Friction Tests

Bollard Runs					
Mode	Pull Mode				
Carriage Velocity (m/s)	0				
Run #1					
RPS	0, 0.01, 0.1, 0.2, 0.5, 1, 2, 3, 4, 5, 11, 12, 13				
Azimuth Angle (deg)	0				
Run #2					
RPS	0, 0.05, 0.1, 0.2, 0.3, 0.4, 0.5				
Azimuth Angle (deg)	0				
Run #3					
RPS	0, 0.01, 0.1, 0.2, 0.5, 1, 2, 3, 4, 5, 11, 12, 13				
Azimuth Angle (deg)	0				
Run #4					
RPS	0, 0.05, 0.1, 0.2, 0.3, 0.4, 0.5				
Azimuth Angle (deg)	0				
Run #5					
RPS	0, 0.01, 0.1, 0.2, 0.5, 1, 2, 3, 4, 5, 11, 12, 13				
Azimuth Angle (deg)	0				
Run #6					
RPS	0, 0.05, 0.1, 0.2, 0.3, 0.4, 0.5				
Azimuth Angle (deg)	0				
Run #7					
RPS	13				
Azimuth Angle (deg)	90				
Run #8					
RPS	13				
Azimuth Angle (deg)	45				

Table 18: General test plan for Bollard Runs

Opens Tests			
Mode	Pull Mode		
Run #1			
Carriage Velocity (m/s)	1.30, 1.56, 1.82, 2.08, 2.34, 2.47, 2.60, 2.86, 3.12		
RPS	13		
Azimuth Angle (deg)	0		

Table 19: General test plan for Opens Tests

Oblique Flow Tests					
Mode	Pull Mode				
Run #1					
Carriage Velocity (m/s)	1.30, 1.56, 1.82, 2.08, 2.34, 2.47, 2.60, 2.86, 3.12				
RPS	13				
Azimuth Angle (deg)	5				
Run #2					
Carriage Velocity (m/s)	1.30, 1.56, 1.82, 2.08, 2.34, 2.47, 2.60, 2.86, 3.12				
RPS	13				
Azimuth Angle (deg)	5				

 Table 20: General test plan for Oblique Flow Tests

6.0 **DESCRIPTION OF EXPERIMENTS**

6.1 Reynolds Number Effect Tests

Flow over full-scale propellers is fully turbulent at operating condition. Flow visualizations on propeller models have found that on model propellers with diameters between 168 and 355mm the boundary layer flow is mainly laminar on both the suction and pressure sides of the propeller blade at propeller $R_n = nD^2/\nu$ below $1*10^6$. Between $R_n = 1*10^6$ and $1*10^7$ the boundary layer develops into fully developed turbulent flow, first on the suction side and then later on the pressure side. The exact or critical R_n at which the flow becomes fully turbulent is dependent on factors such as the geometry, load conditions and flow conditions.⁶

Testing on model propellers must be at rotational speeds that allow the propeller to operate in a flow regime that minimizes laminar flow on the suction side or flow separation on the trailing edge. With respect to podded propulsion open water tests; this flow becomes particularly important in pulling pod configurations because the flow into the propeller is not affected by the turbulent wakes of the strut and pod.⁶

Through open water testing, researchers have found that the propeller performance becomes independent of the R_n at a level where the laminar flow is developing into turbulent flow and this value can be found by completing Reynolds Number Effect Tests.

The performance measurements are Thrust and Torque; the non-dimensional coefficients of Torque and Thrust are K_Q and K_T . If these values are plotted against Reynolds Numbers there will be a point at which the Reynolds numbers does not affect the performance measurements. The performance parameters for both the large (D = 406mm) and small (D = 238mm) propellers stabilize at approximately 1-1.2 *10⁶.

Reynolds effects tests are performed at a number of different Reynolds numbers.



To perform a set of Reynolds effect tests a range of J values are chosen and then tested at a selection of rotation rates. The speed of advance is varied to give a selection of Reynolds Numbers. These Reynolds numbers are then plotted against performance parameters to see if the increase is having a significant effect on performance. The performance parameters are thrust and torque; the non-dimensional coefficients are K_Q and K_T . The equations for both coefficients are shown above.

The following equation is used to determine Reynolds Number:

$$R_n = \frac{c_{0.75}\sqrt{V_A^2 + (0.75\pi nD)^2}}{v}$$

Where: $c_{0.75}$ = Chord length at 0.75 radius fraction of propeller = 0.095m V_A = Speed of advance n = Shaft speed D = Propeller diameter = 0.27m v = Kinematic viscosity = 1.139*10⁻⁶ m²/s

6.2 Air Friction Tests

Conducted by taking the pod(s) out of the water and running them in air. By completing these tests one can estimate the frictional losses in the system. This then allows the researcher to tare the torque values by subtracting this value from all the torque readings measured during the Opens Tests.

6.3 Bollard Runs

These are conducted when the carriage is at a stop. The propeller is run at operating speed (rps); which allows for the computation of Bollard Pull. The Bollard Pull for a propeller is the amount of thrust produced by the propeller when the vessel is stopped. This is particularly important for vessels such as tugboats and icebreakers as they frequently operate at very low, next to zero, velocities.

6.4 **Opens Tests (0 degree azimuth)**

To illustrate the open water performance characteristics of the propeller a plot of K_T , $10K_Q$, η vs. J would be created, this is called the propeller performance chart. The equations to obtain these characteristics are described below in *Table 5*. For clarification, the definitions of all non-dimensional coefficients and terms shown in *Table 5* are explained in further detail in *Table 6*. For completeness efficiency curves would be created and displayed for the data. These curves tend to be more sensitive to errors than thrust and torque coefficients, so therefore more emphasis is placed on observations in the thrust and torque coefficient data.



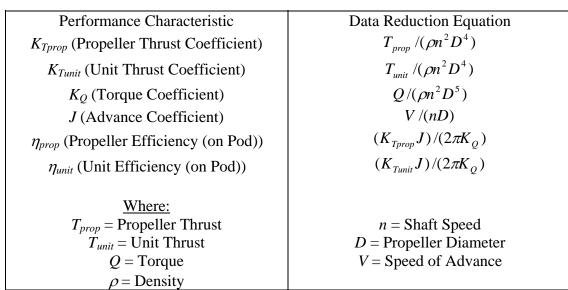


Table 21: Data Reduction Equations used in analysis

	Podded Propeller Test Definition		
K _{Tprop}	Non-dimensional form of the thrust of the propeller installed on the pod		
K _{Tunit}	Non-dimensional form of the unit thrust of the podded propeller		
KQ	Non-dimensional form of the torque on the propeller shaft		
J	Non-dimensional ratio of the advance speed to the shaft speed		
η_{prop}	Open water efficiency of the propeller operating on the pod unit		
η_{unit}	Overall efficiency of the entire pod unit, which factors in the drag of the pod and strut		
Tprop	Axial component of force generated by the propeller when installed on the pod unit		
T _{unit}	Net axial thrust generated by the pod unit; includes the drag of the pod and its influence on		
	the prop		
Q	The axial moment required to rotate the propeller at the desired shaft speed		
Table 22: Definitions of Data Paduation Terms			

Table 22: Definitions of Data Reduction Terms

7.0 DESCRIPTION OF DATA ANALYSIS

For both the tests carried out in the NRC-IOT Ice Tank as well as the test case performed in the MUN Towing Tank ASCII data files were compiled for transfer to researchers personal computers when the trials were completed.

7.1 Interpreting the Raw Data (MUN Towing Tank Tests)

When the data is transferred it is ready to be post-processed. The interpretation was completed using Microsoft Excel 2000. A time series is plotted and averages are taken for each defined section of the run; these final averages are then used in the final analysis. *Figure 19* shows a typical run down the tank while performing an opens test. In the plot below there are four sections; 1^{st} . Nothing is on – both the carriage and propeller are still, 2^{nd} . The carriage is turned on, but still doesn't move forward, 3^{rd} . The prop starts to move at a very low rps while the carriage remains stopped, 4^{th} . The carriage is up to running speed



(approximately 2 m/s below) and the prop is running at desired rps. It should be noted that the plot below does not actually show rps, but shows the reading in volts. This would be changed to rps by multiplying by the appropriate constant.

After the averages are taken for each run the interpreted data can be transferred to a new Excel sheet where it is sorted according to run type (i.e. Third Quadrant Tests, Opens Tests, etc.) and advance coefficient, *J*. The physical quantities can then be non-dimensionalzed using the appropriate expression, as discussed in *Section 7.4*.

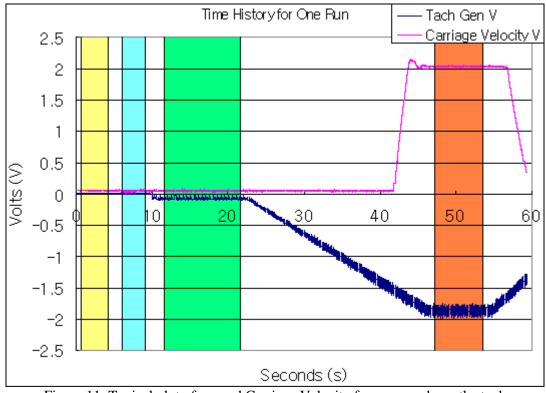


Figure 11: Typical plot of rps and Carriage Velocity for one run down the tank

7.2 Interpreting the Raw Data (NRC-IOT Ice Tank Tests)

Analysis of the tests was on going at the same time as the tests were running. A time series is plotted and averages are taken for each defined section of the run; these final averages are then used in the final analysis. *Figure 24* shows a typical run down the tank while performing an opens test. In the plot below there are three defined sections; 1^{st} . Nothing is on – both the carriage and propeller are still, 2^{nd} . The propeller is up to desired rps (in this case approximately 15), 3^{rd} . The carriage is up to running speed (below at about 3.1 m/s) and the prop is running at desired rps.

After the averages are taken for each run the interpreted data can be transferred to a Microsoft Excel sheet where it is sorted according to run type (i.e. Third Quadrant Tests,



Opens Tests, etc.) and advance coefficient, J (It's customary to sort from J = 0 to J = 1.2). The physical quantities measured can then be non-dimensionalzed using the appropriate expressions, as discussed in *Section* 7.4.

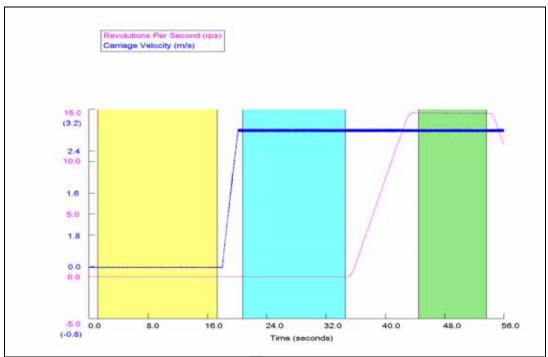
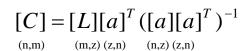


Figure 12: Typical plot of rps and Carriage Velocity for one run down the tank

8.0 CALIBRATIONS

The method used to calibrate the global dynamometer as well as thrust and torque load cells was the linear least squares method. This method theorizes that if enough varied loads are applied in varied directions an accurate estimate of the calibration matrix can be obtained using an optimized linear least square fit. In other words, if the test apparatus can be loaded with enough independent loading cases to cover the expected use of the model during actual testing, then an accurate calibration matrix can be derived.

The algorithm used to obtain the linear least squares calibration matrix is:



Where: n

is the number of balance components

- m is the number of calibration coefficients per component, [m = n(n+3)/2]
- z is the number of loading cases
- [C] contains the calibration coefficients

- [L] defines the calculated distribution of the applied load P between the balance components for each loading case
- [a] defines the actual distribution of the applied load P between the balance components for each loading case

8.1 Global Dynamometer

As stated above, the global dynamometer was calibrated using the linear least squares method. A total of forty-three cases were performed on the test set-up. This provided enough loading cases to provide an accurate calibration matrix.

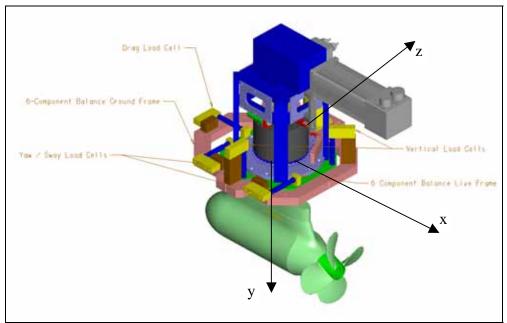


Figure 13: Positive coordinate directions in 3-D space

From the above equation the following matrix of calibration coefficients can be obtained. The calibration coefficients can then be applied directly to the measured data to estimate the actual force reading. [L] and [a] matrices can be found in *Appendix A*.

[C] =	35.065	-0.62753	0.62753	-0.15249	0.08896	0.04254
	4.702	61.447	-61.447	4.7079	-47.924	71.247
	5.2784	24.211	-24.211	5.0931	-49.897	73.751
	0.20125	0.97173	-0.97173	32.769	0.71655	1.5015
	-0.00214	0.72505	-0.72505	-2.8303	36.846	1.6438
	-0.17728	0.20692	-0.20692	-2.5681	0.75165	39.253

8.2 Thrust and Torque Load Cells

Calibrated in much the same way as the global dynamometer. Torque was produced by way of an adapter on the front of the pod where an arm could be attached (figure shown below). The results of the calibration are shown below in tables. [L] and [a] matrices for thrust and torque calibrations can be found in *Appendix B*.

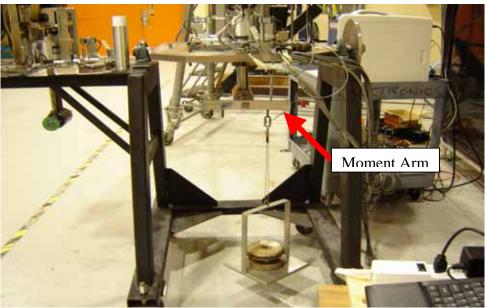


Figure 14: Photo showing how torque can be induced on the system

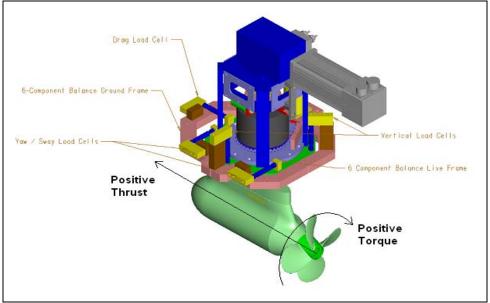


Figure 15: Positive thrust and torque directions during calibrations



From the equation in *Section 8.0* the following matrix of calibration coefficients can be obtained. The calibration coefficients can then be applied directly to the measured data to estimate the actual thrust and torque.

$$\begin{bmatrix} C \end{bmatrix} = \begin{array}{ccc} 65.9407 & 0.0064 \\ 0.0407 & 0.0115 \\ \end{array}$$

9.0 **RESULTS AND DISCUSSION**

In the current study configurations of podded propellers were tested in either the NRC-IOT ice tank or the MUN Towing tank. The propellers were four bladed and in puller configuration. There were also two cases where numerical methods were used to determine the performance characteristics of the podded propeller. The flowing is the results obtained from the Opens Tests along with comments on the experiments performed.

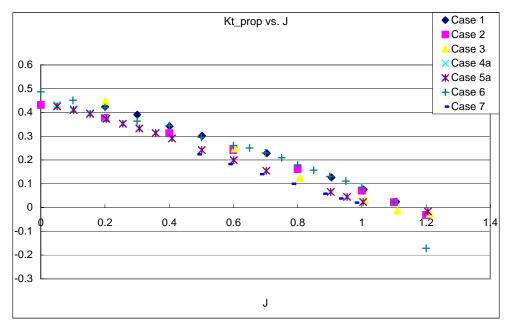


Figure 16: Comparison of K_{T_prop} versus J

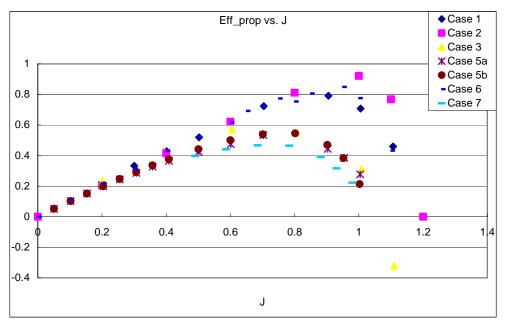


Figure 17: Comparison of $\eta_{_{prop}}$ versus J

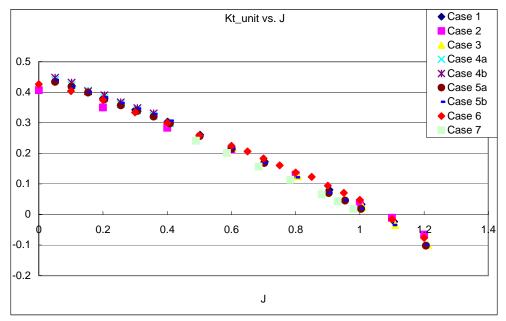


Figure 18: Comparison of K_{T_unit} versus J

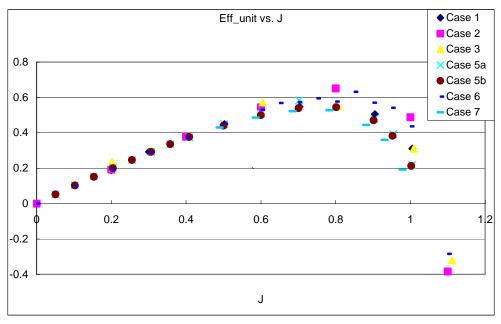


Figure 19: Comparison of η_{unit} versus J

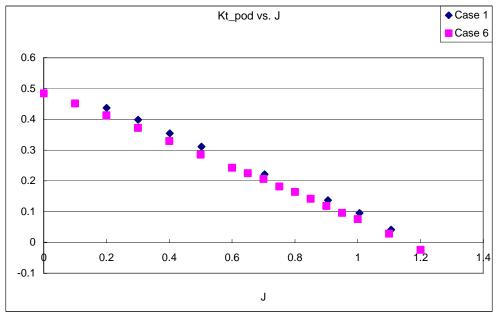


Figure 20: Comparison of K_{T_pod} versus J

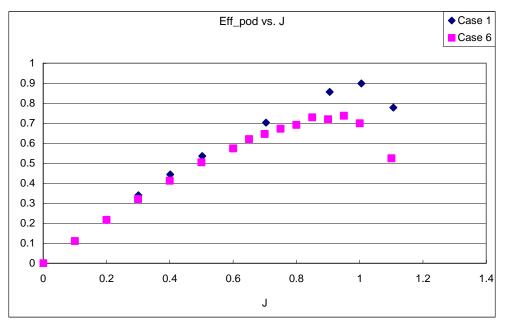


Figure 21: Comparison of $\eta_{\it pod}$ versus J

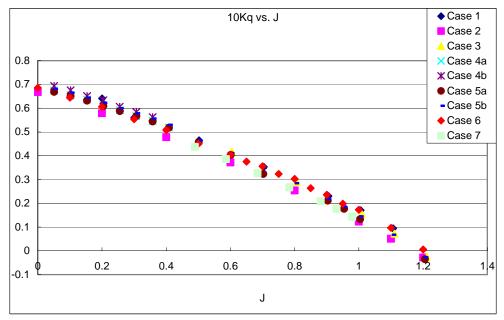


Figure 22: Comparison of 10K_Q versus J

From the above set of plots good comparison can be viewed for K_{T_unit} , K_{T_pod} , and $10K_Q$; with fairly good results for K_{T_prop} . K_{T_prop} : all of the cases go negative between J = 1.05 and 1.15 approximately; K_{T_unit} : all cases go negative between approximately J = 1.05 and 1.1; K_{T_pod} : both cases go negative between J = 1.15 and 1.2; and $10K_Q$: the cases go negative around approximately J = 1.2.

The efficiency curves show poorer quality results than the K_T and $10K_Q$ curves. This could be possibly due to mechanical errors encountered during testing or a whole range of other possible sources. Whatever the cause may be it is not of great concern at this time, as the remainder of the opens tests show promising results; and as was stated earlier emphasis is placed on thrust and torque coefficients.

Unfortunately cases 4a and 4b were not completely finished and therefore it is difficult to compare the results to the rest of the cases. However, from the comparisons that can be made, it looks as though if the runs had been completed it is likely that the trend would have continued and the results would have been similar to the remainder of the results.

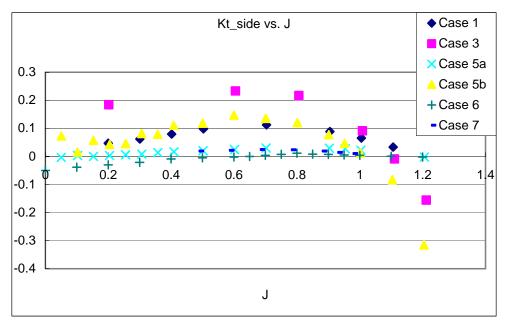


Figure 23: Comparison of K_{T_side} versus J

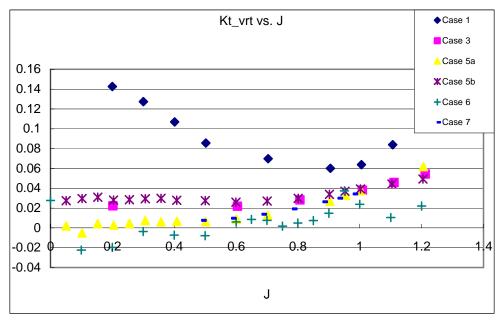


Figure 24: Comparison of K_{T_vrt} versus J

The above two plots are the non-dimensional force coefficients obtained from the global dynamometer. The agreement between the cases isn't very good; however there does seem to be a general trend in each of the plots.

10.0 RECOMMENDATIONS AND CONCLUSIONS

The following is a series of comments on the experiments performed and what steps should be taken in the future to confirm the results obtained.

Overall, the Opens Tests show good results. The tests correspond well with *Principles of Naval Architecture* section on open water tests (page 145).⁵ However, since testing on podded propellers is still not as well know as conventional screw propellers, additional testing should be conducted to compare with this data analyzed. Further testing would provide researchers with valuable knowledge about podded propellers as well as providing a solid base to compare future tests.

Further Reynolds effect tests should be conducted on podded propellers to verify if testing on podded propellers can be completed at lower Reynolds Numbers than recommended by ITTC (i.e. less than $1*10^6$).

Testing thus far by NRC has provided the institute with priceless information and knowledge about the performance characteristics of podded propulsors. Further testing would compliment the testing executed so far and would help to further expand the researcher's knowledge. Plans now being made include the building of a model icebreaker hull to which two podded propellers will be fitted and self-propulsion tests will be conducted.

11.0 ACKNOWLEDGMENTS

I would like to express their gratitude to the National Research Council (NRC) and Memorial University of Newfoundland (MUN) for their financial and other support. Thanks are also extended to the staff in both the Ice tank at Institute for Ocean Technology (IOT) and the staff in the MUN Towing tank, without whose assistance the tests would not have been completed. I would also like to thank Dr. Ayhan Akinturk, whose support and guidance throughout my work term has allowed me to expand my engineering knowledge.

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APPENDIX A: Calibration Data for Global Dynamometer

					1					
0.000195	a ₁₂	-0.000002	a _{1 3}	-0.000324	a ₁₄	-0.014440	a ₁₅	0.009645	a ₁₆	0.031223
0.000203	a ₂₂	-0.000092	a ₂₃	-0.000196	a ₂₄	-0.018068	a ₂₅	0.022992	a ₂₆	0.021882
0.000217	a ₃₂	-0.000170	a _{3 3}	-0.000059	a ₃₄	-0.014240	a ₃₅	0.032529	a ₃₆	0.009249
0.000216	a ₄₂	-0.000239	a _{4 3}	0.000063	a _{4 4}	-0.004432	a 4 5	0.036409	a ₄₆	-0.003590
0.020020	a ₅₂	0.000525	a _{5 3}	-0.000728	a ₅₄	0.018484	a _{5 5}	0.005772	a ₅₆	-0.003839
0.019963	a ₆₂	-0.006626	a ₆₃	0.006172	a ₆₄	0.015276	a ₆₅	0.013996	a ₆₆	-0.008683
0.019914	a ₇₂	-0.012950	a _{7 3}	0.012284	a ₇₄	0.015068	a _{7 5}	0.021208	a ₇₆	-0.015380
0.019877	a ₈₂	-0.016941	a ₈₃	0.016174	a ₈₄	0.020498	a ₈₅	0.025721	a ₈₆	-0.024769
0.028344	a ₉₂	-0.000764	a 9 3	0.000544	a 94	0.034327	a ₉₅	-0.000415	a ₉₆	-0.032013
0.028194	a _{10 2}	-0.014058	a _{10 3}	0.013405	a ₁₀₄	0.034140	a _{10 5}	-0.000459	a ₁₀₆	-0.031759
0.028117	a _{11 2}	-0.024495	a _{11 3}	0.023504	a _{11 4}	0.032846	a _{11 5}	-0.000490	a ₁₁₆	-0.030490
0.028090	a _{12 2}	-0.027440	a _{12 3}	0.026370	a ₁₂₄	0.033828	a ₁₂₅	-0.000502	a ₁₂₆	-0.031385
-0.019738	a ₁₃₂	-0.000275	a _{13 3}	-0.000008	a ₁₃₄	-0.038168	a ₁₃₅	0.005998	a ₁₃₆	0.049189
-0.019698	a _{14 2}	0.010259	a _{14 3}	-0.010146	a _{14 4}	-0.040563	a _{14 5}	0.018221	a ₁₄₆	0.039655
-0.019731	a _{15 2}	0.015956	a _{15 3}	-0.015600	a ₁₅₄	-0.035808	a _{15 5}	0.024800	a ₁₅₆	0.028816
-0.019746	a _{16 2}	0.016634	a _{16 3}	-0.016238	a ₁₆₄	-0.026980	a _{16 5}	0.025666	a ₁₆₆	0.019722
-0.028211	a _{17 2}	-0.000968	a _{17 3}	0.000681	a ₁₇₄	-0.034967	a _{17 5}	-0.000371	a ₁₇₆	0.032725
-0.028311	a _{18 2}	-0.014139	a _{18 3}	0.013359	a ₁₈₄	-0.034467	a ₁₈₅	-0.000213	a ₁₈₆	0.032102
-0.028385	a ₁₉₂	-0.024052	a _{19 3}	0.022892	a ₁₉₄	-0.034383	a ₁₉₅	-0.000095	a ₁₉₆	0.031908
-0.028418	a _{20 2}	-0.027663	a _{20 3}	0.026368	a ₂₀₄	-0.034127	a _{20 5}	-0.000048	a ₂₀₆	0.031622
0.000057	a _{21 2}	-0.000042	a _{21 3}	-0.000181	a ₂₁₄	0.023576	a ₂₁₅	-0.018298	a ₂₁₆	0.022486
0.000329	a _{22 2}	0.000155	a _{22 3}	-0.000452	a _{22 4}	-0.023445	a _{22 5}	0.008822	a ₂₂₆	0.040493
0.000261	a _{23 2}	-0.000034	a _{23 3}	-0.000258	a ₂₃₄	-0.029015	a _{23 5}	0.028406	a ₂₃₆	0.026982
0.000213	a _{24 2}	-0.000215	a _{24 3}	-0.000053	a _{24 4}	-0.023606	a _{24 5}	0.041982	a ₂₄₆	0.008951
0.000139	a _{25 2}	-0.000339	a _{25 3}	0.000111	a _{25 4}	-0.009037	a _{25 5}	0.047180	a ₂₅₆	-0.009609
0.000015	a _{26 2}	-0.000066	a _{26 3}	-0.000159	a _{26 4}	0.029226	a _{26 5}	-0.029007	a _{26 6}	0.027356
0.020077	a _{27 2}	-0.000223	a _{27 3}	-0.000021	a _{27 4}	0.011221	a _{27 5}	0.006718	a ₂₇₆	0.001966
0.019971	a _{28 2}	-0.010421	a _{28 3}	0.009842	a ₂₈₄	0.007381	a _{28 5}	0.018352	a ₂₈₆	-0.005547
0.019851	a _{29 2}	-0.018892	a _{29 3}	0.018062	a _{29 4}	0.009533	a _{29 5}	0.027997	a ₂₉₆	-0.016769
0.019215	a _{30 2}	-0.023189	a _{30 3}	0.022280	a _{30 4}	0.018896	a _{30 5}	0.033847	a ₃₀₆	-0.030591
0.028280	a _{31 2}	0.000682	a _{31 3}	-0.000855	a ₃₁₄	0.033118	a _{31 5}	-0.000177	a ₃₁₆	-0.030320
0.028144	a _{32 2}	-0.017098	a _{32 3}	0.016404	a ₃₂₄	0.032827	a _{32 5}	0.000180	a ₃₂₆	-0.030297
	0.000203 0.000217 0.000216 0.020020 0.019963 0.019914 0.019877 0.028344 0.028194 0.028194 0.028194 0.028197 0.028090 -0.019738 -0.019738 -0.019738 -0.019746 -0.028311 -0.028311 -0.028311 -0.028311 -0.028311 0.000057 0.0028311 0.000057 0.000329 0.000261 0.000213 0.000015 0.000015 0.000015 0.019971 0.019851 0.019215 0.028280	0.000203 a22 0.000217 a32 0.000216 a42 0.000216 a42 0.000200 a52 0.019963 a62 0.019963 a62 0.019963 a62 0.019963 a62 0.019964 a72 0.019877 a82 0.028344 a92 0.028117 a112 0.028090 a122 -0.019738 a132 -0.019738 a132 -0.019738 a142 -0.019738 a152 -0.019739 a152 -0.019731 a152 -0.028311 a182 -0.028311 a182 -0.028311 a122 -0.028418 a202 0.000057 a212 0.0000261 a232 0.0000139 a252 0.0000139 a262 0.019971 a262 0.019971 a292 0.019971 <td>0.000203 a_{22} -0.000092 0.000217 a_{32} -0.000170 0.000216 a_{42} -0.000239 0.020020 a_{52} 0.000525 0.019963 a_{62} -0.006626 0.019914 a_{72} -0.012950 0.019877 a_{82} -0.016941 0.028344 a_{92} -0.000764 0.028194 a_{12} -0.014058 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td=""><td>$0.000203$$a_{22}$$-0.000092$$a_{23}$$-0.000196$$a_{24}$$-0.018068$$a_{25}$$0.000217$$a_{32}$$-0.000170$$a_{33}$$-0.000059$$a_{34}$$-0.014240$$a_{35}$$0.000216$$a_{42}$$-0.000239$$a_{43}$$0.000063$$a_{44}$$-0.004432$$a_{45}$$0.02020$$a_{52}$$0.000525$$a_{53}$$-0.00728$$a_{54}$$0.018484$$a_{55}$$0.019914$$a_{72}$$-0.006266$$a_{63}$$0.006172$$a_{64}$$0.015276$$a_{65}$$0.019914$$a_{72}$$-0.012950$$a_{73}$$0.012284$$a_{74}$$0.015088$$a_{75}$$0.019877$$a_{82}$$-0.016941$$a_{83}$$0.016174$$a_{84}$$0.024948$$a_{85}$$0.028344$$a_{92}$$-0.00764$$a_{93}$$0.00544$$a_{94}$$0.034327$$a_{95}$$0.028117$$a_{112}$$-0.024495$$a_{113}$$0.023504$$a_{114}$$0.032846$$a_{115}$$0.028000$$a_{122}$$-0.027440$$a_{123}$$0.026370$$a_{124}$$0.033828$$a_{125}$$-0.019738$$a_{132}$$-0.00275$$a_{133}$$-0.00008$$a_{134}$$-0.038168$$a_{155}$$-0.019746$$a_{162}$$0.016344$$a_{163}$$-0.01638$$a_{164}$$-0.034167$$a_{155}$$-0.028311$$a_{152}$$-0.027663$$a_{203}$$0.022892$$a_{194}$$-0.034183$$a_{155}$$-$</td><td>0.000203 a22 -0.000092 a23 -0.00105 a24 -0.018068 a25 0.022992 0.000217 a32 -0.000239 a43 -0.00055 a34 -0.014240 a35 0.032529 0.000216 a42 -0.000239 a43 0.000078 a44 -0.014432 a45 0.036409 0.002002 a52 0.000525 a53 -0.000728 a54 0.018484 a55 0.00577 0.019963 a62 -0.006626 a63 0.012284 a74 0.015068 a75 0.021208 0.019877 a52 -0.016941 a53 0.016174 a64 0.034327 a55 -0.00415 0.028109 a12 -0.014058 a103 0.013405 a104 0.034284 a15 -0.00490 0.02809 a12 -0.027440 a123 0.026370 a144 -0.03488 a15 0.00598 0.019731 a15 -0.00275 a133 -0.01638 a144 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td=""><td>$0.000203$$a_{22}$$-0.000092$$a_{23}$$-0.000196$$a_{24}$$-0.018068$$a_{25}$$0.000217$$a_{32}$$-0.000170$$a_{33}$$-0.000059$$a_{34}$$-0.014240$$a_{35}$$0.000216$$a_{42}$$-0.000239$$a_{43}$$0.000063$$a_{44}$$-0.004432$$a_{45}$$0.02020$$a_{52}$$0.000525$$a_{53}$$-0.00728$$a_{54}$$0.018484$$a_{55}$$0.019914$$a_{72}$$-0.006266$$a_{63}$$0.006172$$a_{64}$$0.015276$$a_{65}$$0.019914$$a_{72}$$-0.012950$$a_{73}$$0.012284$$a_{74}$$0.015088$$a_{75}$$0.019877$$a_{82}$$-0.016941$$a_{83}$$0.016174$$a_{84}$$0.024948$$a_{85}$$0.028344$$a_{92}$$-0.00764$$a_{93}$$0.00544$$a_{94}$$0.034327$$a_{95}$$0.028117$$a_{112}$$-0.024495$$a_{113}$$0.023504$$a_{114}$$0.032846$$a_{115}$$0.028000$$a_{122}$$-0.027440$$a_{123}$$0.026370$$a_{124}$$0.033828$$a_{125}$$-0.019738$$a_{132}$$-0.00275$$a_{133}$$-0.00008$$a_{134}$$-0.038168$$a_{155}$$-0.019746$$a_{162}$$0.016344$$a_{163}$$-0.01638$$a_{164}$$-0.034167$$a_{155}$$-0.028311$$a_{152}$$-0.027663$$a_{203}$$0.022892$$a_{194}$$-0.034183$$a_{155}$$-$</td><td>0.000203 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-0.0</td><td>$0.000203$$a_{22}$$0.000190$$a_{24}$$0.018068$$a_{25}$$0.022929$$a_{26}$$0.000217$$a_{32}$$0.000170$$a_{33}$$0.000059$$a_{34}$$0.014240$$a_{35}$$0.032529$$a_{36}$$0.000216$$a_{42}$$0.000239$$a_{43}$$0.000053$$a_{44}$$0.014343$$a_{45}$$0.036409$$a_{46}$$0.020020$$a_{52}$$0.000525$$a_{53}$$0.000728$$a_{54}$$0.018484$$a_{55}$$0.005772$$a_{56}$$0.019963$$a_{62}$$0.006266$$a_{63}$$0.006172$$a_{64}$$0.015276$$a_{65}$$0.012980$$a_{76}$$0.019977$$a_{52}$$0.006764$$a_{93}$$0.006174$$a_{84}$$0.02498$$a_{55}$$0.021208$$a_{76}$$0.028144$$a_{92}$$0.000764$$a_{93}$$0.006144$$a_{94}$$0.034140$$a_{105}$$0.000490$$a_{116}$$0.028177$$a_{112}$$0.02498$$a_{113}$$0.02370$$a_{14}$$0.033284$$a_{115}$$0.000490$$a_{116}$$0.028177$$a_{123}$$0.00275$$a_{133}$$0.00008$$a_{14}$$0.033828$$a_{125}$$0.000490$$a_{166}$$0.028177$$a_{132}$$0.014608$$a_{144}$$0.033828$$a_{125}$$0.00598$$a_{166}$$0.028177$$a_{133}$$0.00275$$a_{144}$$0.033828$$a_{125}$$0.00598$$a_{166}$$0.019778$$a_{12}$$0.00275$</td></t<>	0.000203 a_{22} -0.000092 a_{23} -0.000196 a_{24} -0.018068 a_{25} 0.000217 a_{32} -0.000170 a_{33} -0.000059 a_{34} -0.014240 a_{35} 0.000216 a_{42} -0.000239 a_{43} 0.000063 a_{44} -0.004432 a_{45} 0.02020 a_{52} 0.000525 a_{53} -0.00728 a_{54} 0.018484 a_{55} 0.019914 a_{72} -0.006266 a_{63} 0.006172 a_{64} 0.015276 a_{65} 0.019914 a_{72} -0.012950 a_{73} 0.012284 a_{74} 0.015088 a_{75} 0.019877 a_{82} -0.016941 a_{83} 0.016174 a_{84} 0.024948 a_{85} 0.028344 a_{92} -0.00764 a_{93} 0.00544 a_{94} 0.034327 a_{95} 0.028117 a_{112} -0.024495 a_{113} 0.023504 a_{114} 0.032846 a_{115} 0.028000 a_{122} -0.027440 a_{123} 0.026370 a_{124} 0.033828 a_{125} -0.019738 a_{132} -0.00275 a_{133} -0.00008 a_{134} -0.038168 a_{155} -0.019746 a_{162} 0.016344 a_{163} -0.01638 a_{164} -0.034167 a_{155} -0.028311 a_{152} -0.027663 a_{203} 0.022892 a_{194} -0.034183 a_{155} $-$	0.000203 a22 -0.000092 a23 -0.00105 a24 -0.018068 a25 0.022992 0.000217 a32 -0.000239 a43 -0.00055 a34 -0.014240 a35 0.032529 0.000216 a42 -0.000239 a43 0.000078 a44 -0.014432 a45 0.036409 0.002002 a52 0.000525 a53 -0.000728 a54 0.018484 a55 0.00577 0.019963 a62 -0.006626 a63 0.012284 a74 0.015068 a75 0.021208 0.019877 a52 -0.016941 a53 0.016174 a64 0.034327 a55 -0.00415 0.028109 a12 -0.014058 a103 0.013405 a104 0.034284 a15 -0.00490 0.02809 a12 -0.027440 a123 0.026370 a144 -0.03488 a15 0.00598 0.019731 a15 -0.00275 a133 -0.01638 a144 -0.0	0.000203 a_{22} 0.000190 a_{24} 0.018068 a_{25} 0.022929 a_{26} 0.000217 a_{32} 0.000170 a_{33} 0.000059 a_{34} 0.014240 a_{35} 0.032529 a_{36} 0.000216 a_{42} 0.000239 a_{43} 0.000053 a_{44} 0.014343 a_{45} 0.036409 a_{46} 0.020020 a_{52} 0.000525 a_{53} 0.000728 a_{54} 0.018484 a_{55} 0.005772 a_{56} 0.019963 a_{62} 0.006266 a_{63} 0.006172 a_{64} 0.015276 a_{65} 0.012980 a_{76} 0.019977 a_{52} 0.006764 a_{93} 0.006174 a_{84} 0.02498 a_{55} 0.021208 a_{76} 0.028144 a_{92} 0.000764 a_{93} 0.006144 a_{94} 0.034140 a_{105} 0.000490 a_{116} 0.028177 a_{112} 0.02498 a_{113} 0.02370 a_{14} 0.033284 a_{115} 0.000490 a_{116} 0.028177 a_{123} 0.00275 a_{133} 0.00008 a_{14} 0.033828 a_{125} 0.000490 a_{166} 0.028177 a_{132} 0.014608 a_{144} 0.033828 a_{125} 0.00598 a_{166} 0.028177 a_{133} 0.00275 a_{144} 0.033828 a_{125} 0.00598 a_{166} 0.019778 a_{12} 0.00275

A-1: Matrix of coefficients obtained from measured data ([a] matrix)



	0.020026		0 020006		0.029790		0.022006		0.000456		0.020720
a_{331}	0.028026	a _{33 2}	-0.030886	a 33 3	0.029790	a _{33 4}	0.032006	a _{33 5}	0.000456	a ₃₃₆	-0.029720
a _{34 1}	0.028040	a _{34 2}	-0.029491	a _{34 3}	0.028441	a _{34 4}	0.032729	a _{34 5}	0.000435	a ₃₄₆	-0.030377
a _{35 1}	0.028527	a _{35 2}	0.029442	a _{35 3}	-0.028780	a _{35 4}	0.034110	a _{35 5}	-0.000845	a ₃₅₆	-0.030813
a ₃₆₁	-0.020171	a _{36 2}	0.000493	a _{36 3}	-0.000663	a ₃₆₄	0.007872	a _{36 5}	0.007335	a ₃₆₆	0.004525
a _{37 1}	-0.020194	a _{37 2}	-0.012607	a _{37 3}	0.011942	a _{37 4}	0.012466	a _{37 5}	-0.007498	a ₃₇₆	0.014456
a _{38 1}	-0.019379	a _{38 2}	0.018198	a _{38 3}	-0.017706	a _{38 4}	-0.037984	a _{38 5}	0.027990	a ₃₈₆	0.028190
a _{39 1}	-0.019522	a _{39 2}	0.020608	a _{39 3}	-0.020022	a ₃₉₄	-0.028954	a _{39 5}	0.030784	a ₃₉₆	0.016922
a _{40 1}	-0.028262	a _{40 2}	-0.001292	a _{40 3}	0.001015	a _{40 4}	-0.033571	a _{40 5}	-0.000138	a ₄₀₆	0.031957
a _{41 1}	-0.028133	a_{412}	0.015615	a _{41 3}	-0.015197	a _{41 4}	-0.034279	a _{41 5}	0.000035	a ₄₁₆	0.032476
a_{421}	-0.028425	a_{422}	-0.026347	a _{42 3}	0.025061	a_{424}	-0.033592	a _{42 5}	-0.000433	a ₄₂₆	0.032207
a _{43 1}	-0.028444	a _{43 2}	-0.029187	a _{43 3}	0.027782	a _{43 4}	-0.034047	a _{43 5}	-0.000482	a ₄₃₆	0.032664

Matrix of coefficients obtained from measured data

f ₁₁	0.000000	f_{12}	0.000000	f ₁₃	0.000000	f ₁₄	-0.532872	f ₁₅	0.352286	f ₁₆	1.180636
f ₂₁	0.000000	f ₂₂	0.000000	f ₂₃	0.000000	f _{2 4}	-0.657899	f ₂₅	0.831907	f ₂₆	0.826042
f ₃₁	0.000000	f ₃₂	0.000000	f 33	0.000000	f ₃₄	-0.519859	f35	1.183014	f ₃₆	0.336895
f ₄₁	0.000000	f _{4 2}	0.000000	f _{4 3}	0.000000	f _{4 4}	-0.155739	f _{4 5}	1.311528	f ₄₆	-0.155739
f ₅₁	0.707135	f _{5 2}	0.000000	f _{5 3}	0.000000	f _{5 4}	0.467414	f 55	0.249101	f ₅₆	-0.009380
f ₆₁	0.707135	f 6 2	-0.301072	f _{6 3}	0.301072	f _{6 4}	0.379007	f ₆₅	0.588241	f ₆₆	-0.260113
f ₇₁	0.707135	f _{7 2}	-0.521473	f _{7 3}	0.521473	f _{7 4}	0.476615	f 7 5	0.836509	f ₇₆	-0.605989
f ₈₁	0.707135	f _{8 2}	-0.602145	f _{8 3}	0.602145	f ₈₄	0.734085	f ₈₅	0.927381	f ₈₆	-0.954331
f 91	1.000050	f 92	0.000000	f 93	0.000000	f 94	1.193901	f95	0.000000	f ₉₆	-1.193901
f _{10 1}	1.000050	f _{10 2}	-0.425785	f _{10 3}	0.425785	f _{10 4}	1.193901	f _{10 5}	0.000000	f ₁₀₆	-1.193901
f _{11 1}	1.000050	f _{11 2}	-0.737481	f _{11 3}	0.737481	f _{11 4}	1.193901	f _{11 5}	0.000000	f _{11 6}	-1.193901
f _{12 1}	1.000050	f _{12 2}	-0.851093	f _{12 3}	0.851093	f _{12 4}	1.193901	f _{12 5}	0.000000	f _{12 6}	-1.193901
f ₁₃₁	-0.707135	f ₁₃₂	0.000000	f _{13 3}	0.000000	f _{13 4}	-1.221001	f _{13 5}	0.249101	f ₁₃₆	1.679035
f _{14 1}	-0.707135	f _{14 2}	0.301072	f _{14 3}	-0.301072	f _{14 4}	-1.309408	f _{14 5}	0.588241	f _{14 6}	1.428302
f _{15 1}	-0.707135	f ₁₅₂	0.521473	f _{15 3}	-0.521473	f _{15 4}	-1.211800	f _{15 5}	0.836509	f ₁₅₆	1.082426
f _{16 1}	-0.707135	f _{16 2}	0.602145	f _{16 3}	-0.602145	f _{16 4}	-0.954331	f _{16 5}	0.927381	f _{16 6}	0.734085
f _{17 1}	-1.000050	f _{17 2}	0.000000	f _{17 3}	0.000000	f _{17 4}	-1.193901	f _{17 5}	0.000000	f ₁₇₆	1.193901
f _{18 1}	-1.000050	f ₁₈₂	-0.425785	f _{18 3}	0.425785	f _{18 4}	-1.193901	f _{18 5}	0.000000	f ₁₈₆	1.193901
f ₁₉₁	-1.000050	f ₁₉₂	-0.737481	f _{19 3}	0.737481	f _{19 4}	-1.193901	f ₁₉₅	0.000000	f ₁₉₆	1.193901
f _{20 1}	-1.000050	f _{20 2}	-0.851570	f _{20 3}	0.851570	f _{20 4}	-1.193901	f _{20 5}	0.000000	f ₂₀₆	1.193901
f _{21 1}	0.000000	f _{21 2}	0.000000	f _{21 3}	0.000000	f _{21 4}	0.803503	f _{21 5}	-0.606956	f _{21 6}	0.803503
f _{22 1}	0.000000	f _{22 2}	0.000000	f _{22 3}	0.000000	f _{22 4}	-0.895679	f _{22 5}	0.352286	f _{22 6}	1.543442
f _{23 1}	0.000000	f _{23 2}	0.000000	f _{23 3}	0.000000	f _{23 4}	-1.073651	f _{23 5}	1.035011	f ₂₃₆	1.038690
f _{24 1}	0.000000	f _{24 2}	0.000000	f _{24 3}	0.000000	f _{24 4}	-0.877155	f _{24 5}	1.534800	f _{24 6}	0.342405
f _{25 1}	0.000000	f _{25 2}	0.000000	f _{25 3}	0.000000	f _{25 4}	-0.358843	f _{25 5}	1.717735	f _{25 6}	-0.358843
f _{26 1}	0.000000	f _{26 2}	0.000000	f _{26 3}	0.000000	f _{26 4}	1.006606	f _{26 5}	-1.013163		1.006606
f _{27 1}	0.707135	f _{27 2}	0.000000	f _{27 3}	0.000000	f _{27 4}	0.268720	f _{27 5}	0.249101	f ₂₇₆	0.189314
f _{28 1}	0.707135	f _{28 2}	-0.428567	f _{28 3}	0.428567	f _{28 4}	0.085029	f _{28 5}	0.731856	f ₂₈₆	-0.109750
f _{29 1}	0.707135	f _{29 2}	-0.742299	f _{29 3}	0.742299	f _{29 4}	0.223971	f _{29 5}	1.085257	f ₂₉₆	-0.602093
f _{30 1}	0.707135	f _{30 2}	-0.857133	f _{30 3}	0.857133	f _{30 4}	0.590470	f _{30 5}	1.214610	f ₃₀₆	-1.097945
f _{31 1}	1.000050	f _{31 2}	0.000000	f _{31 3}	0.000000	f _{31 4}	1.193901	f _{31 5}	0.000000	f _{31 6}	-1.193901
f _{32 1}	1.000050	f _{32 2}	-0.606091	f _{32 3}	0.606091	f _{32 4}	1.193901	f _{32 5}	0.000000	f _{32 6}	-1.193901

A-2: Matrix of coefficients obtained from calculated data ([L] matrix)

f _{33 1}	1.000050	f _{33 2}	-1.128514	f33 3	1.128514	f _{33 4}	1.193901	f _{33 5}	0.000000	f _{33 6}	-1.193901
f _{34 1}		f _{34 2}	-1.115207			f _{34 4}		f _{34 5}		f _{34 6}	-1.193901
f _{35 1}		f _{35 2}		f _{35 3}	-1.115207			f _{35 5}		f _{35 6}	-1.193901
f _{36 1}	-0.707135			f _{36 3}		f _{36 4}		f _{36 5}		f _{36 6}	0.247160
f _{37 1}	-0.707135		-0.428567			f _{37 4}		f _{37 5}	-0.233653		0.567784
f _{38 1}	-0.707135			f _{38 3}	-0.682915	-	-1.396504			f _{38 6}	1.085275
f _{39 1}	-0.707135			f _{39 3}	-0.857133		-1.097945			f _{39 6}	0.590470
f _{40 1}	-1.000050			1393 f ₄₀₃		1394 f ₄₀₄	-1.193901			f _{40 6}	1.193901
	-1.000050				-0.606091		-1.193901				1.193901
f _{41 1} f	-1.000050		-1.049780	f _{41 3} f						f _{41 6} f	1.193901
ք _{42 1} ք						ք _{42 4} բ	-1.193901			f _{42 6} ¢	
f_{431}	-1.000050	L 43 2	-1.212181	143 3	1.212181	f _{43 4}	-1.193901	f _{43 5}	0.000000	f ₄₃₆	1.193901

Matrix of coefficients obtained from calculated data

APPENDIX B: Calibration Data for Thrust and Torque Load Cells

a ₁₁	0.008517	a ₁₂	4.799733
a ₂₁	-0.010700	a ₂₂	-4.780244
a ₃₁	-0.000339	a ₃₂	6.713952
a ₄₁	-0.000337	a ₄₂	-6.676090
a ₅₁	0.014632	a ₅₂	0.001815
a ₆₁	-0.015982	a ₆₂	-0.000193
a ₇₁	-0.016897	a _{7 2}	-0.002923
a ₈₁	0.014210	a ₈₂	-0.003161

B-1: Matrix of coefficients obtained from measured data

Matrix of coefficients obtained from measured data

f ₁₁	0.707100	f ₁₂	0.053881
f_{21}	-0.707100	f ₂₂	-0.053881
f ₃₁	0.000000	f ₃₂	0.076200
f ₄₁	0.000000	f _{4 2}	-0.076200
f ₅₁	1.000000	f _{5 2}	0.000000
f ₆₁	-1.000000	f _{6 2}	0.000000
f ₇₁	-1.000000	f _{7 2}	0.000000
f ₈₁	1.000000	f _{8 2}	0.000000

B-2: Matrix of coefficients obtained from calculated data

Matrix of coefficients obtained from calculated data

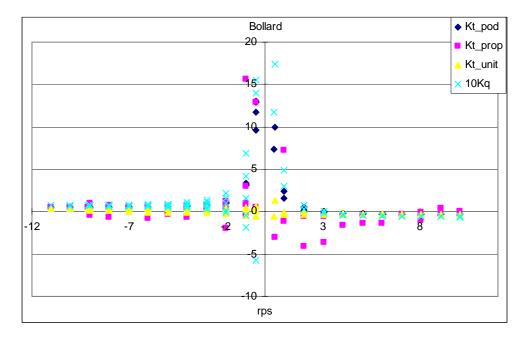
APPENDIX C: Data Acquisition System Channel Set-up for NRC-IOT Tests

C-1: Channel Set-up

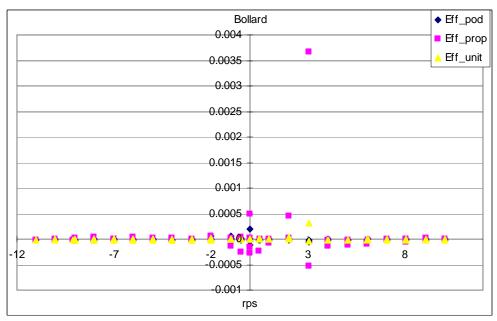
					DAS PLAN									
	Project Name: T.C. Azipod									Project Number: 42_2085_16				
		Signa	al Conditioner: Custom IOTe	ch					Date: 9-Dec-05					
	Sampling Rate: 5Khz								rated by: Ja	ames E. Willia	ms			
GDAC	CHAN #	IOTech#	DESCRIPTION/DEVICE	SERIAL #	BAR-CODE	RANGE	FILTER	EXC. Volts	Gain	Offset	Cal. Factor			
1	0	Ch00-0-0	Pod 1, Fxa, Port	E50407	200203	250 lbf	1Khz	10	150					
2	1	Ch00-0-1	Pod 1, Fy1a	E50185	200201	250 lbf	1Khz	10	150					
3	2	Ch00-0-2	Pod 1, Fy2a	E50406	200207	250 lbf	1Khz	10	150					
4	3	Ch00-0-3	Pod 1, Fz1a	E50400	200204	250 lbf	1Khz	10	150					
5	4	Ch00-0-4	Pod 1, Fz2a	E50204	200205	250 lbf	1Khz	10	150					
6	5	Ch00-0-5	Pod 1, FZ3a	E50184	200208	250 lbf	1Khz	10	150					
7	6	Ch00-0-6	spare				1Khz	5						
8	7	Ch00-0-7	spare				1Khz	5						
9	8	Ch00-1-0	Pod 2, Fxb, Starboard	E50413	200206	250 lbf	1Khz	10	150					
10	9	Ch00-1-1	Pod 2, Fy1b	E50384	200198	250 lbf	1Khz	10	150					
11	10	Ch00-1-2	Pod 2, Fy2b	E50170	200199	250 lbf	1Khz	10	150					
12	11	Ch00-1-3	Pod 2, Fz1b	E50417	200200	250 lbf	1Khz	10	150					
13	12	Ch00-1-4	Pod 2, Fz2b	E50403	200197	250 lbf	1Khz	10	150					
14	13	Ch00-1-5	Pod 2, FZ3b	E50194	200202	250 lbf	1Khz	10	150					
15	14	Ch00-1-6	spare				1Khz	5						
16	15	Ch00-1-7	spare				1Khz	5						
17	16	Ch01-0-0	Pod 1, Thrust, Ta	21316		50 lbf	1Khz	N/A	4.4					
18	17	Ch01-0-1	Pod 1, Torque, Qa	А			1Khz	N/A	5.39					
19	18	Ch01-0-2	Pod 1 RPS				1Khz	N/A	?					

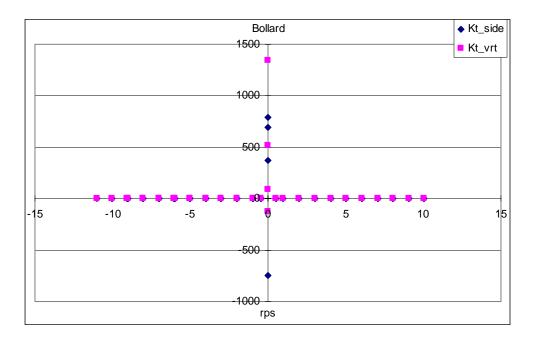
20	19	Ch01-0-3				1Khz	N/A			
21	20	Ch01-1-0	Pod 2 Thrust ,Tb	21320	50 lbf	1Khz	N/A	3.45		
22	21	Ch01-1-1	Pod 2, Torque,Qb	В		1Khz	N/A	5.39		
23	22	Ch01-1-2	Pod 2 RPS			1Khz	N/A	?		
24	23	Ch01-1-3	DAS Sync signal			1Khz	N/A			
25		RS232 Ch1	Pod 1 Azimithing angle		360 degs	na				
26		RS232 Ch2	Pod 2 Azumithing angle		360 degs	na				
27		RS232 Ch3	Pod 1 Blade Angle							
28		RS232 Ch4	Pod 2 Blade Angle							
29		RS232 Ch5	Pod 1 RPS							
30		RS232 Ch6	Pod 2 RPS							
30		RS232 Ch7	DAS Sync signal							
			Industrial pc:	Telem # : PC004026	IP #		Barcode:			
			Daq book:	S/N:	Barcode:					

APPENDIX D: Results for Case One

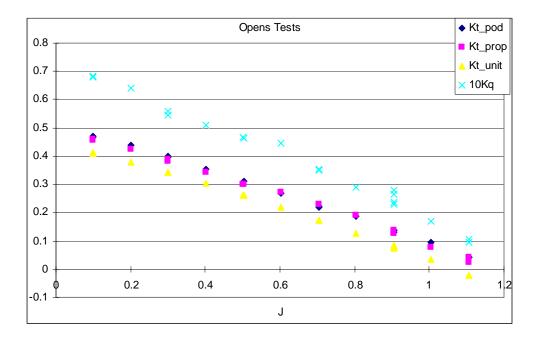


D-1: Reynolds Number Effect Tests

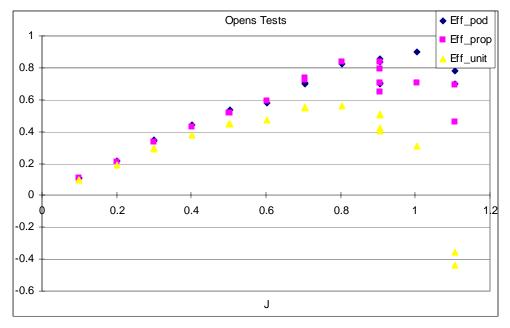


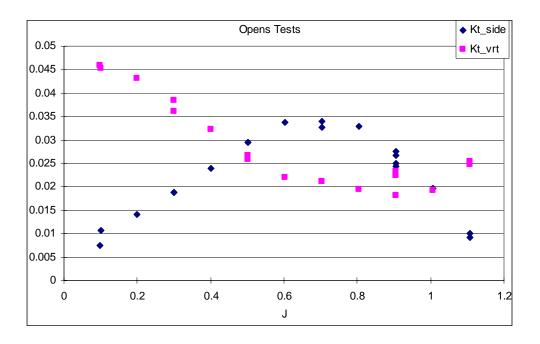


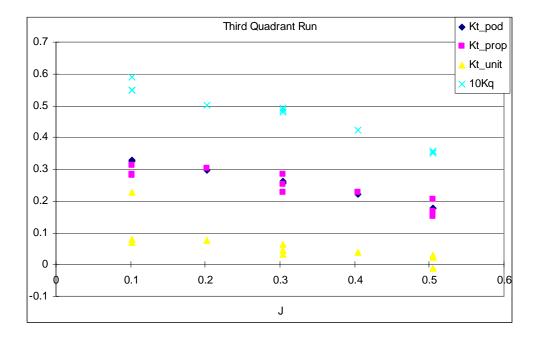
D-3



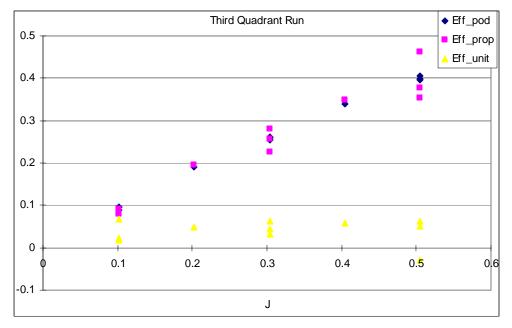
D-2: Opens Tests Results

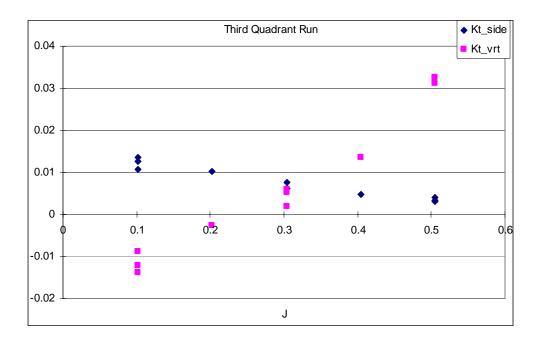




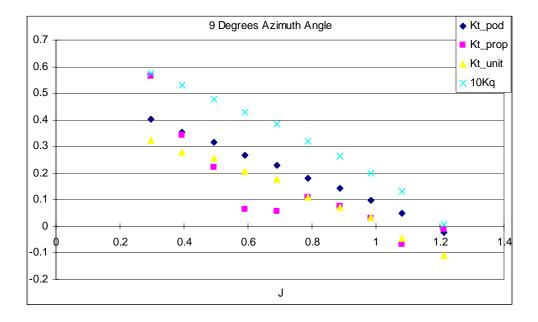


D-3: Third Quadrant Runs

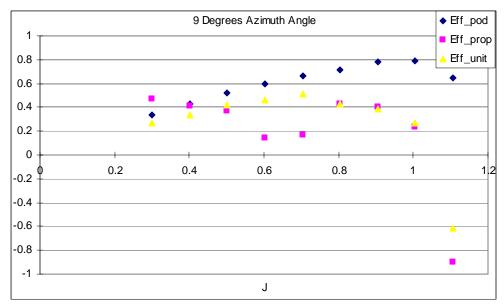


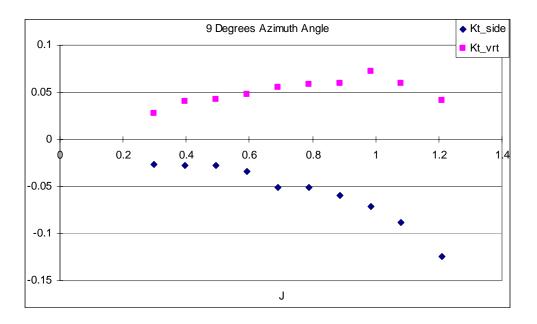


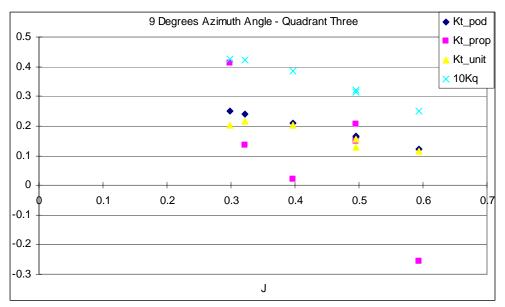
D-7

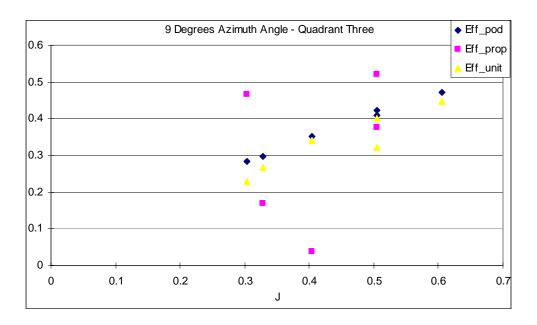


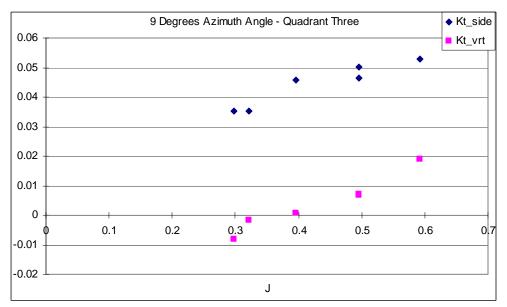
D-4: Oblique Flow Tests

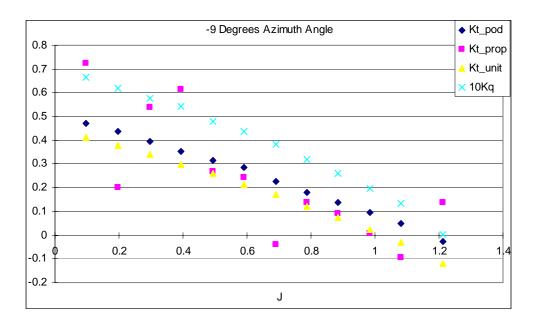


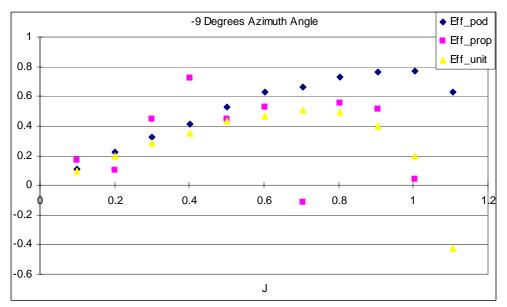


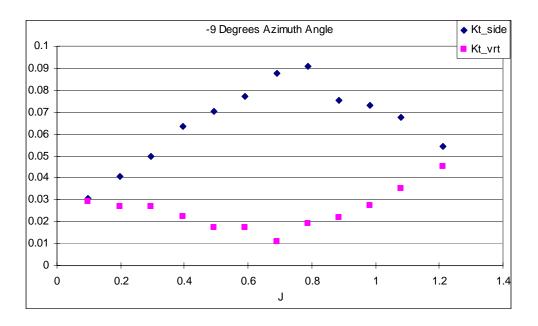


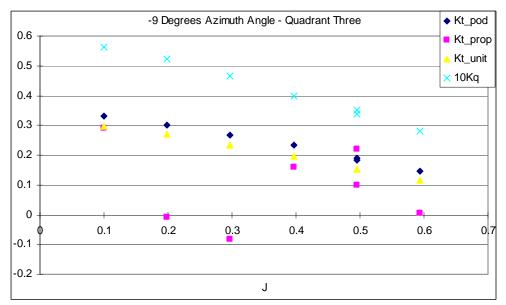


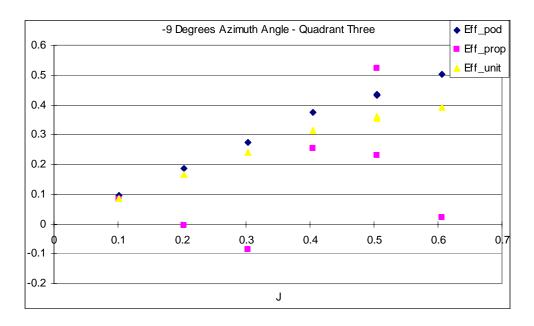


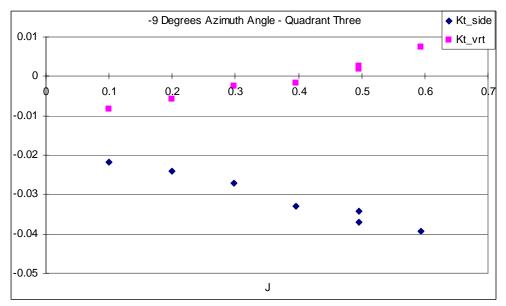




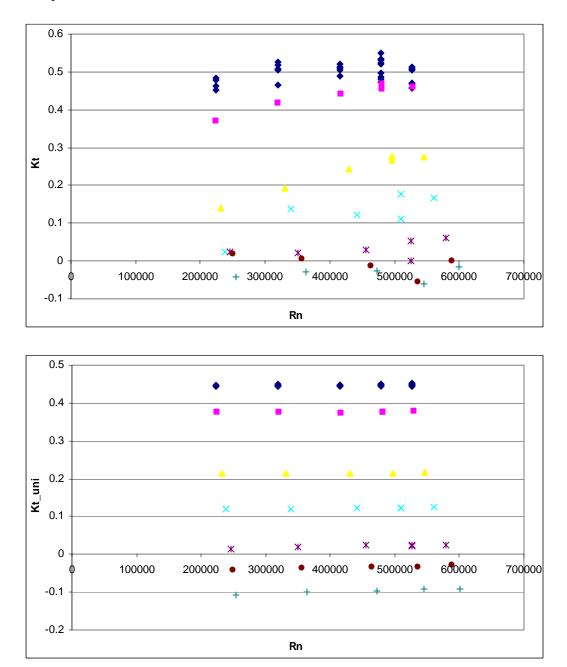




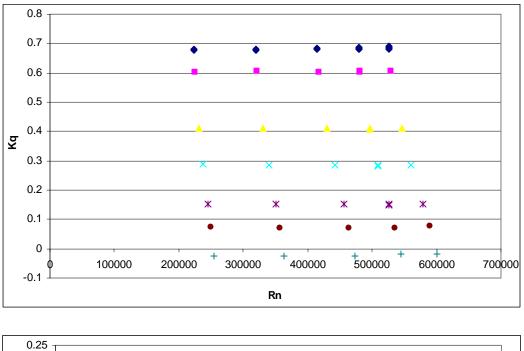


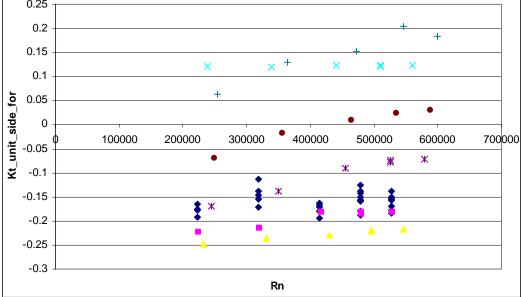


APPENDIX E: Results for Case Three

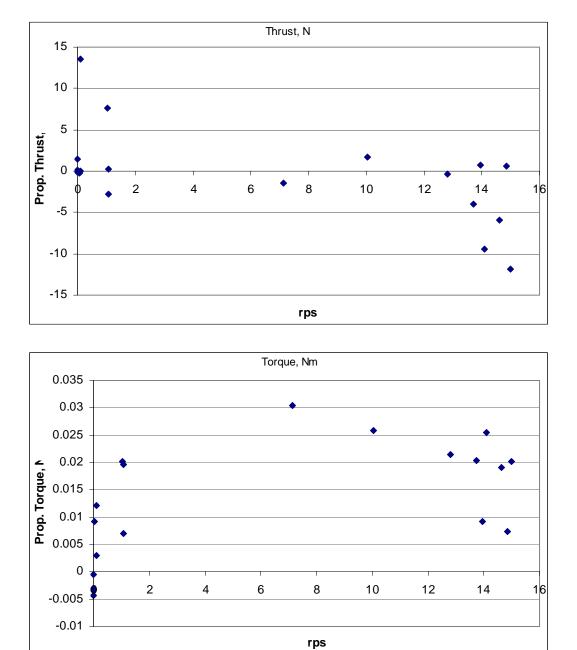


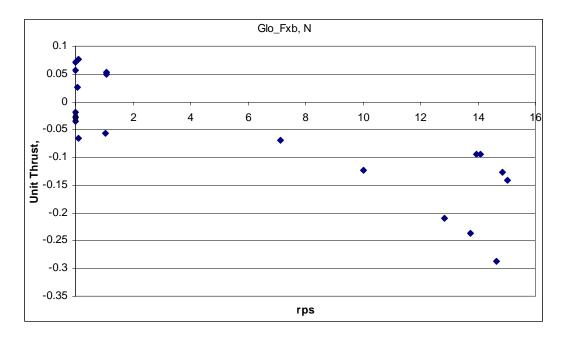
E-1: Reynolds Number Effect Tests

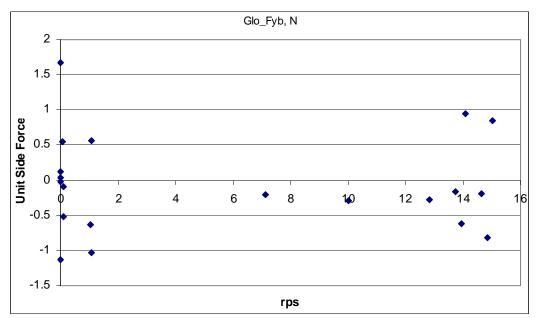




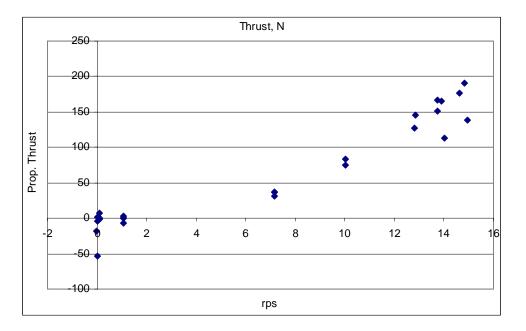


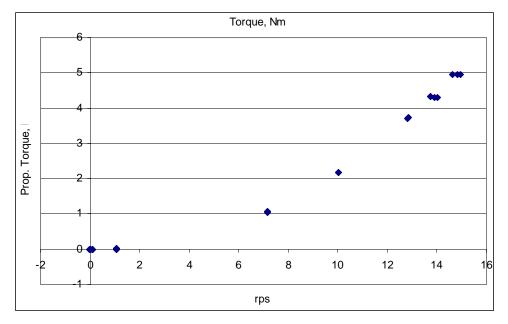


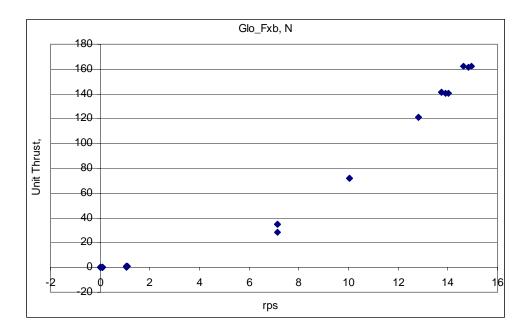


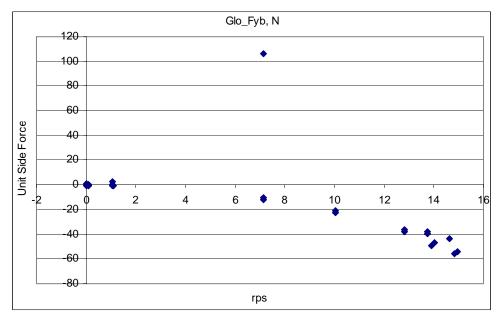


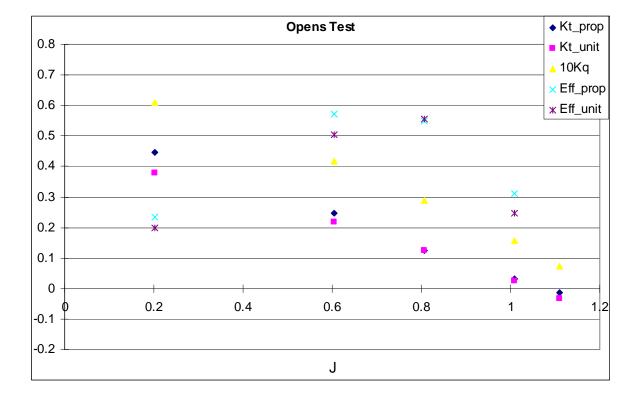
E-3: Bollard Runs





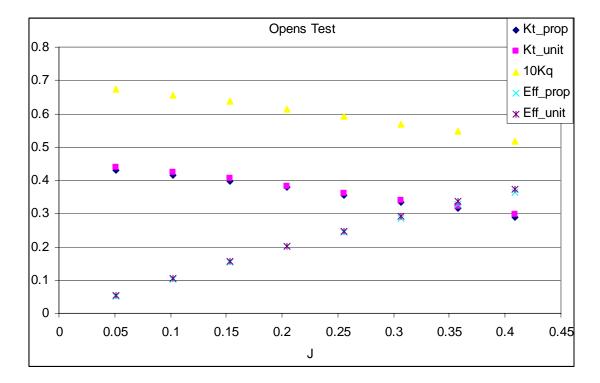




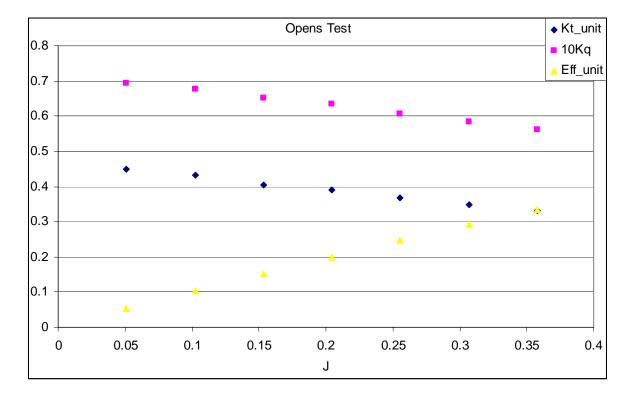


E-4: Opens Tests

APPENDIX F: Results for Case 4



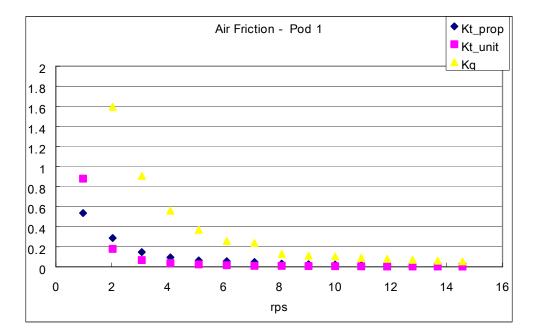
F-1: Opens Tests (Case 4a)

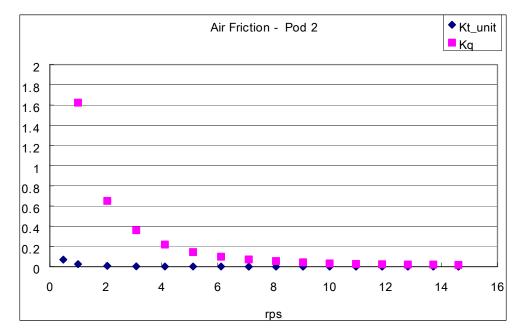


F-2: Opens Tests (Case 4b)

APPENDIX G: Results for Case 5

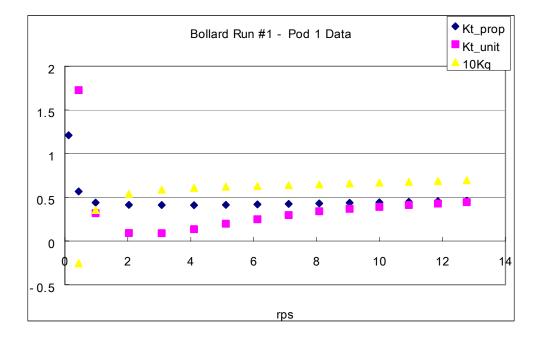
G-1: Air Friction Tests

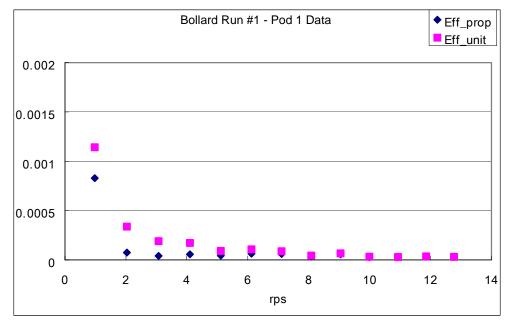


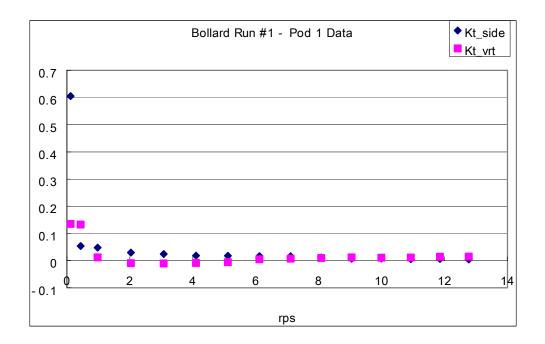


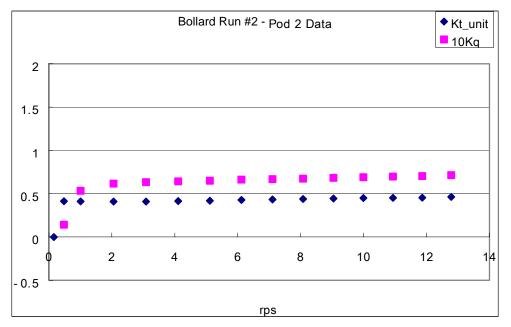


G-2: Bollard Runs

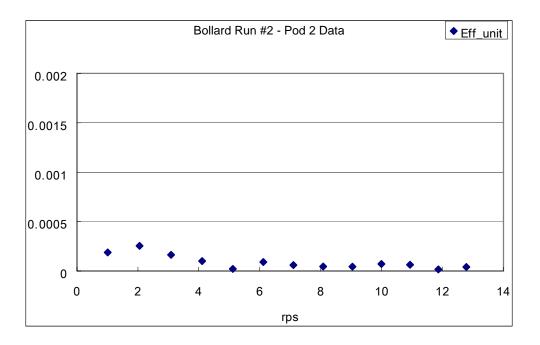


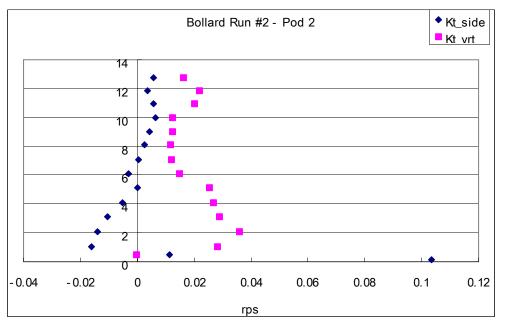


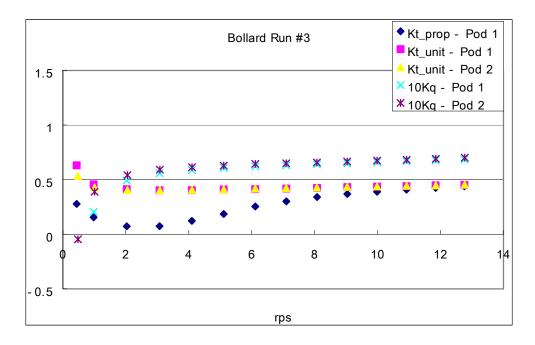


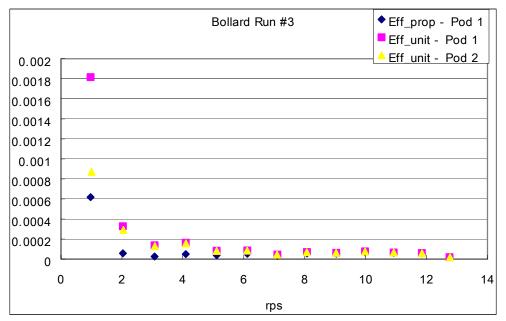


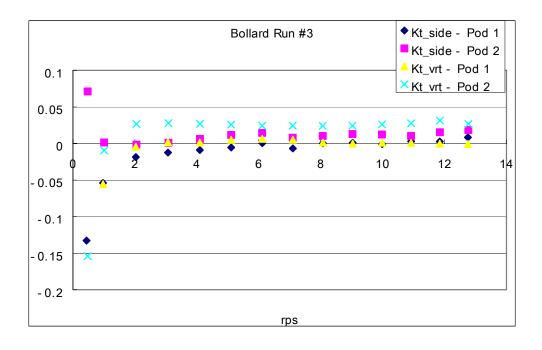
NAC-CNAC





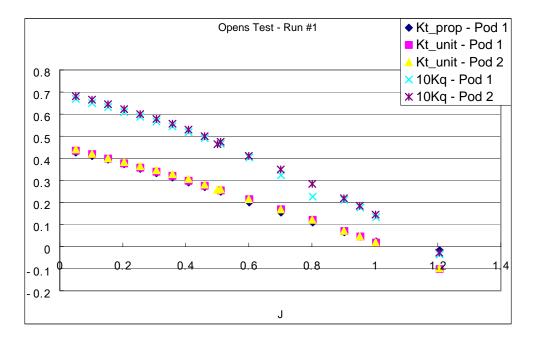


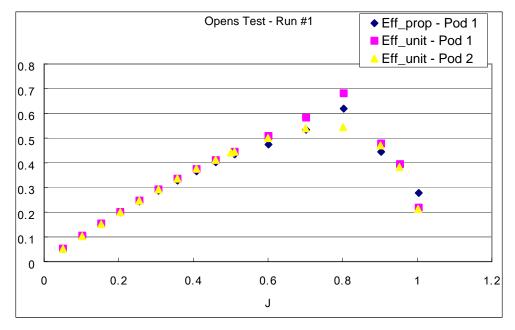


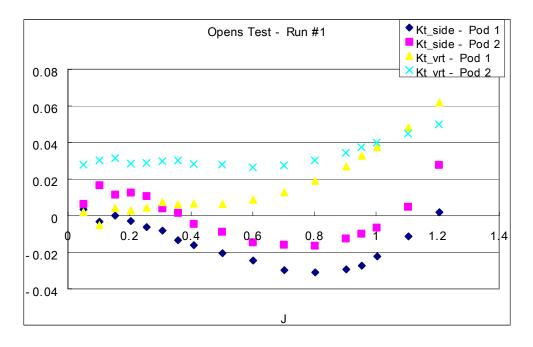


G-7

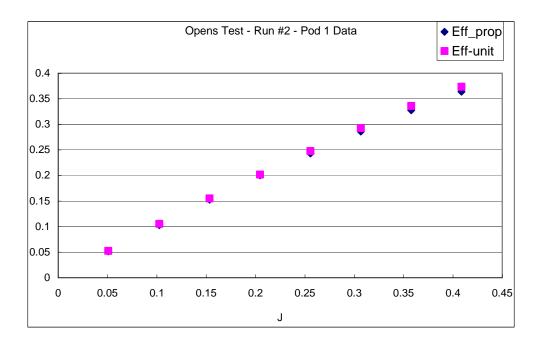


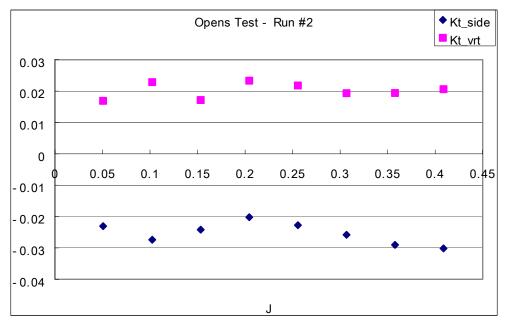


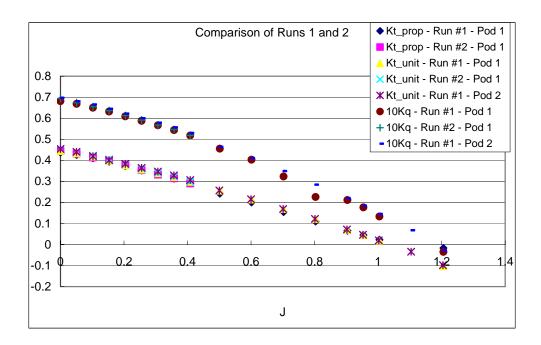


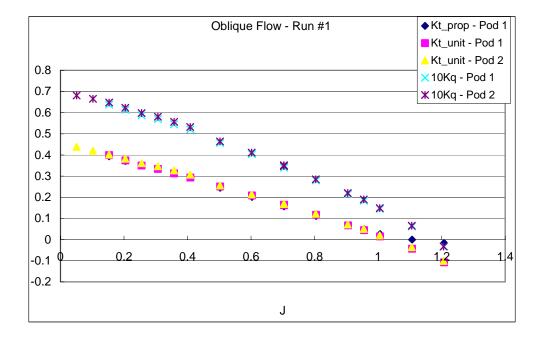




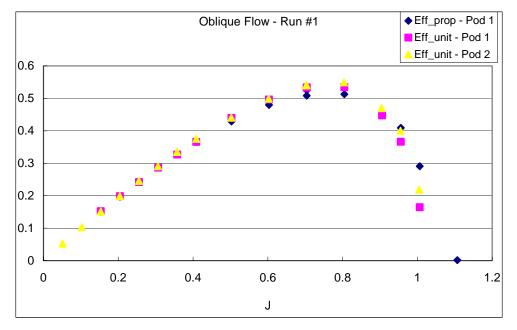




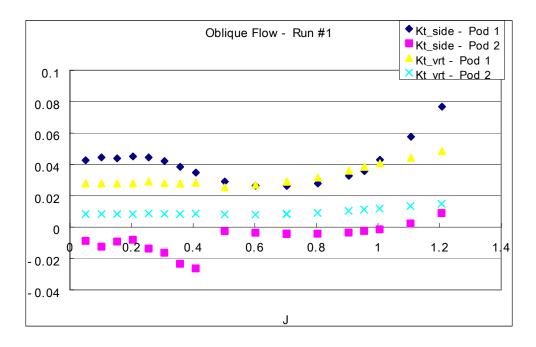


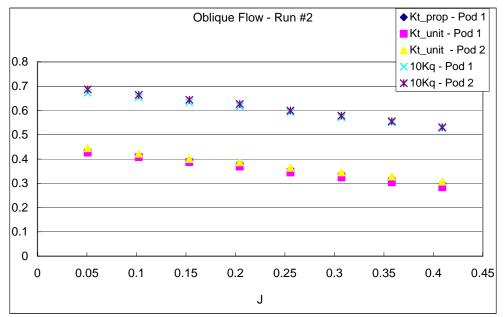


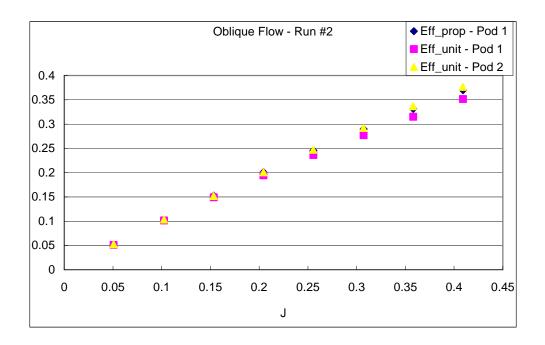
G-4: Oblique Flow Tests

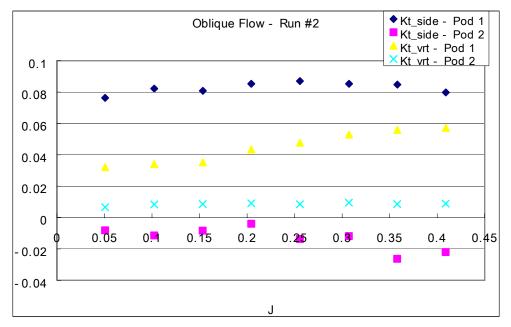


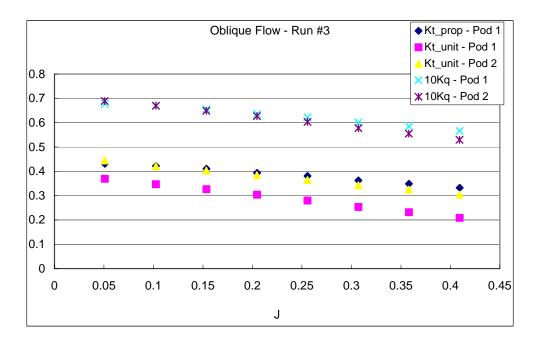


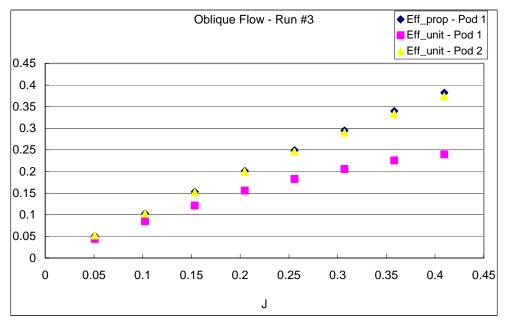


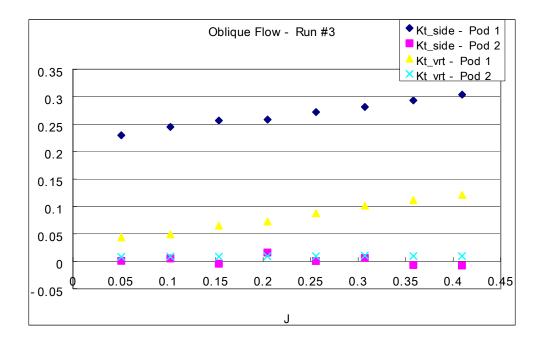


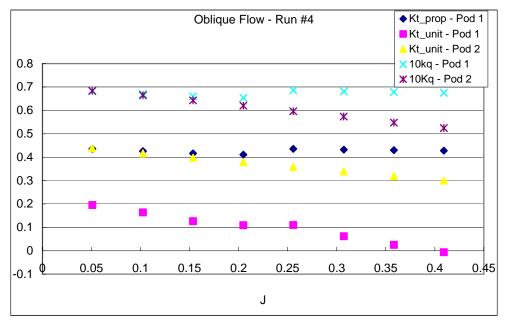


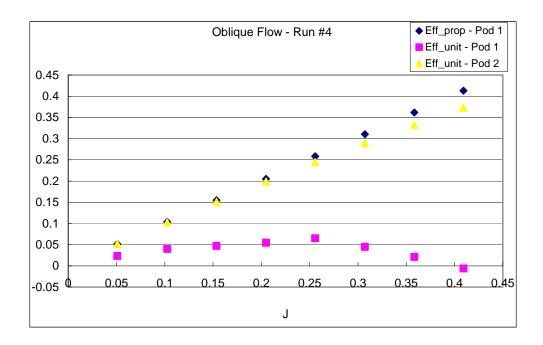


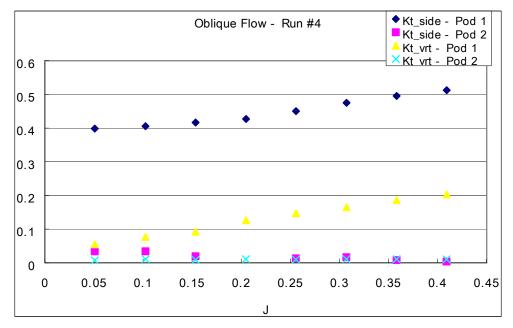


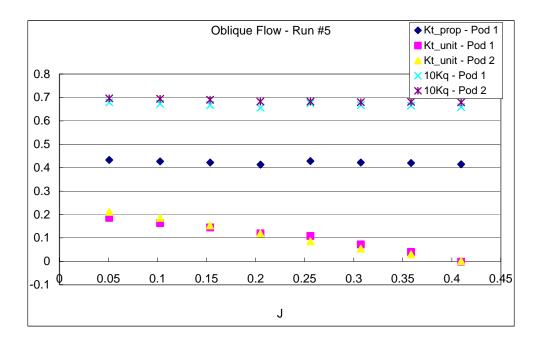


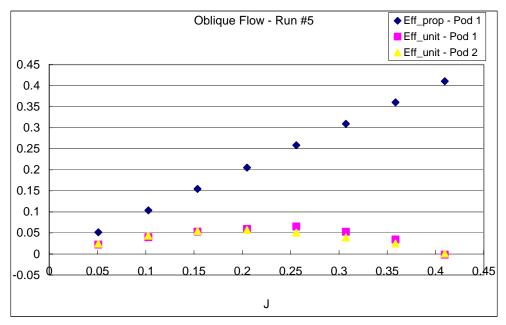


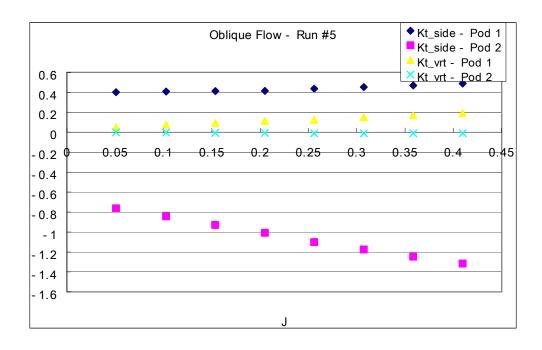




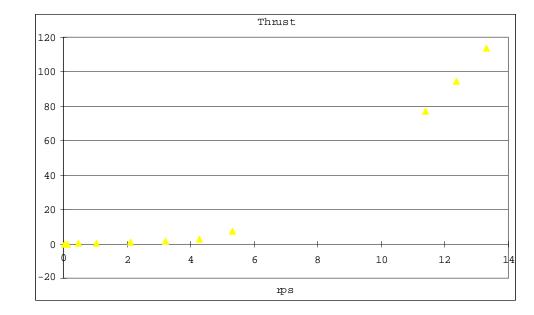




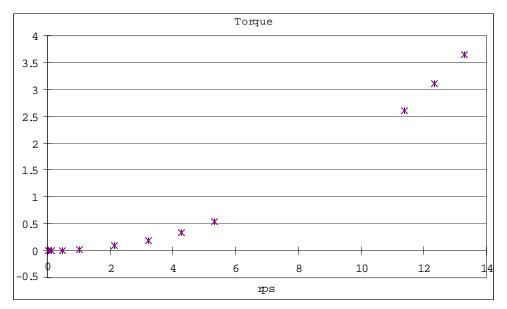


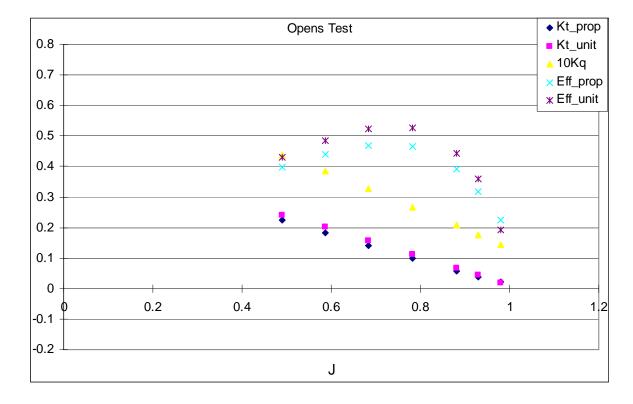


APPENDIX H: Results for Case Seven



H-1: Bollard Runs





H-2: Opens Tests