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Preferential Alignment of Incommensurate Block Copolymer Dot Arrays Forming Moiré Superstructures

Cong Jin,^{†,‡} Brian C. Olsen,^{†,‡} Erik J. Lubber,^{*,†,‡} and Jillian M. Buriak^{*,†,‡}

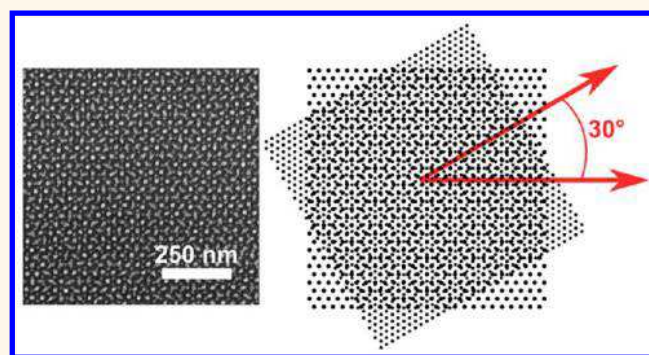
[†]Department of Chemistry, University of Alberta, 11227 Saskatchewan Drive, Edmonton, Alberta T6G 2G2, Canada

[‡]National Institute for Nanotechnology, National Research Council Canada, 11421 Saskatchewan Drive, Edmonton, Alberta T6G 2M9, Canada

S Supporting Information

ABSTRACT: Block copolymer (BCP) self-assembly is of great interest as a cost-effective method for large-scale, high-resolution nanopattern fabrication. Directed self-assembly can induce long-range order and registration, reduce defect density, and enable access to patterns of higher complexity. Here we demonstrate preferential orientation of two incommensurate BCP dot arrays. A bottom layer of hexagonal silica dots is prepared *via* typical self-assembly from a PS-*b*-PDMS block copolymer. Self-assembly of a second, or top, layer of a different PS-*b*-PDMS block copolymer that forms a hexagonal dot pattern with different periodicity results in a predictable moiré superstructure. Four distinct moiré superstructures were demonstrated through a combination of different BCPs and different order of annealing. The registration force of the bottom layer of hexagonal dots is sufficient to direct the self-assembly of the top layer to adopt a preferred relative angle of rotation. Large-area helium ion microscopy imaging enabled quantification of the distributions of relative rotations between the two lattices in the moiré superstructures, yielding statistically meaningful results for each combination. It was also found that if the bottom layer dots were too large, the resulting moiré pattern was lost. A small reduction in the bottom layer dot size, however, resulted in large-area moiré superstructures, suggesting a specific size regime where interlayer registration forces can induce long-range preferential alignment of incommensurate BCP dot arrays.

KEYWORDS: moiré superstructure, block copolymer, self-assembly, incommensurate, heteroepitaxy, sequential deposition, nanopattern



Self-assembly of block copolymers (BCPs) into functional nanopatterns has been the focus of much attention as a potential candidate for next-generation nanolithography.^{1–5} Block copolymers are composed of two or more chemically distinct polymer chains, connected *via* covalent bonds.^{1,6,7} By tuning their molecular weight, chemical composition, and volume fraction of the blocks, thin films can spontaneously form periodic nanopatterns on surfaces, including arrays of parallel lines, hexagonal dot patterns, and linear lamellae, upon annealing.^{8–11} The pattern of the self-assembled periodic polymeric nanostructures can then be transferred to the underlying substrate *via* physical methods^{12–15} or converted to another material, such as metal, carbon, a metal oxide, and a sulfide, through chemical transformation.^{14,16–24} Compared to commercial optical lithography, nanopatterning *via* self-assembly of BCPs has the potential for lower cost, with high resolution.^{25–28}

Directed self-assembly (DSA) is of great interest to induce long-range order, orientation, and registry of BCP nanopatterns and to reduce the incidence of defects.^{4,8,9,22,29–41} DSA is an epitaxial approach that relies upon sparse prepatterning of a substrate with chemical or topological features to guide the process of BCP self-assembly in a spatially defined manner.^{42–44} DSA has been demonstrated to yield low-defect, periodic patterns with long-range order,^{29,32,45–47} as well as complex patterns such as bands,⁴⁸ jogs,⁴⁹ T-junctions,⁴⁹ concentric circles,¹⁷ square arrays,^{50,51} and some 3D nanopatterns.⁵² With respect to the application of DSA to dot patterns, arrays of chemical and topological dot patterns, prepared by e-beam lithography, have been most commonly used.^{29,45,53} For instance, chemical patterns with varying feature

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densities from 1:1 to more sparse arrangements have been shown to exert control over orientational order.^{32,54,55} Ross and co-workers showed that hexagonal arrays of ~ 30 -nm-high pillars of silica could substitute (act as surrogates) for minority domains within hexagonal ordered BCPs,⁴⁵ if the pillars had a spacing that was a multiple of the periodicity of the BCP pattern (an integral multiple of L_0).^{56,57} Trenches and other hole arrays, also produced *via* e-beam lithography, have been used to direct the long-range order of BCP dot patterns,^{56,58–61} as well as the use of nanoimprint lithography stamps.⁴⁴

Using only bottom-up methods, commensurate assembly of a second BCP pattern directed by a first can produce hierarchical topographical nanopatterns^{62–64} or metal/metal-oxide binary nanoarrays.^{65–67} While promising, these exploratory examples are still few, and little work has been done to statistically quantify the epitaxially alignment produced using these bottom-up methods. In our recent work,⁶⁸ we described the use of an array of hexagonal silica dots, prepared *via* self-assembly of BCPs of PS-*b*-PDMS, to direct the self-assembly of a top layer of a thin film of the same PS-*b*-PDMS BCP. The commensurate, two-layered pattern was converted to a honeycomb pattern of silica dots with a concomitant doubling of the density of the dots. In this article, nanoscale structures produced *via* sequential deposition of self-assembled BCP hexagonal dot arrays with incommensurate periodicity are investigated. It is found that a unique set of preferential orientation relationship(s) exist between the two BCP dot arrays, leading to formation of moiré superstructures not previously observed in directed self-assembly. Previously, arbitrarily oriented moiré structures and labyrinth-like nanopatterns had been observed by TEM when free-standing monolayers of self-assembled hexagonal dot array BCP films were folded onto themselves, forming a bilayer.⁶⁹ In the work described here, the resulting moiré superstructures are driven by registration between the bottom and top layers, leading to large multi-micrometer-sized grains with preferred, majority phases. Although it is unclear what applications will make use of these BCP moiré superstructures, they may prove to be useful as photonic metasurfaces with tunable optical properties.⁷⁰

RESULTS AND DISCUSSION

The general scheme for the self-assembly of incommensurate BCP double layers is shown in Figure 1. The bottom layer of hexagonal dots is formed *via* self-assembly of a PS-*b*-PDMS BCP, followed by solvent annealing and reactive ion etching (RIE) to transform the BCP into the nanopattern of silica dots (Figure 1a). A second layer of a PS-*b*-PDMS BCP, which has a different molecular weight and thus a different periodicity, is then spin-coated onto the initial pattern of silica dots (bottom layer). Upon a second solvent anneal (Figure 1c) and RIE treatment, the top layer of the PS-*b*-PDMS BCP is converted into another array of dots (Figure 1d). The resulting nanopattern is generally a moiré superstructure.

In this work, the two different PS-*b*-PDMS BCPs and BCP blend used in this study, and their abbreviations, are summarized in Table 1. These BCPs were chosen in order to explore a large range of array pitches and pitch ratios. The B30 blend was specifically chosen to achieve a large pitch of 43 nm (blending was necessary to produce dot arrays instead of cylindrical arrays).²⁰ The plan view scanning electron micrographs (SEM) and atomic force micrographs (AFM) of single-layer silica dot patterns fabricated from B30, P43, and P22 on flat silicon substrates are shown in Figures S1 and S2

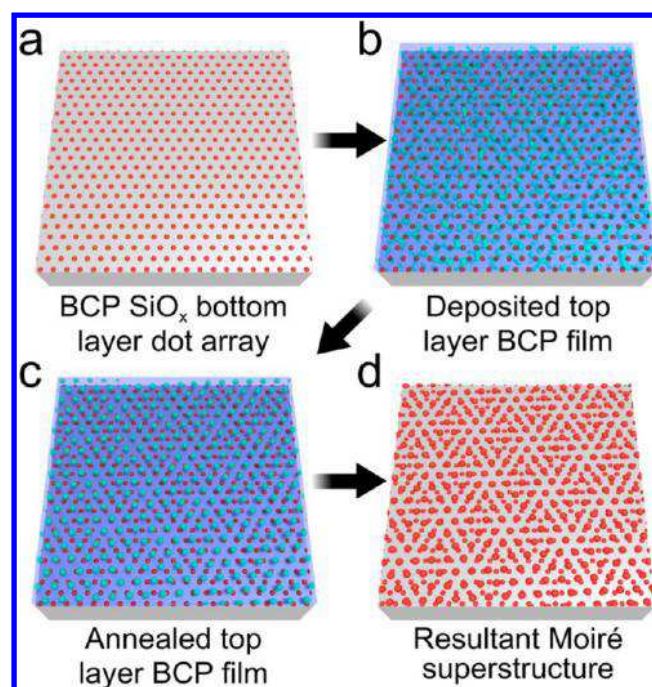


Figure 1. Schematic illustrating the method for formation of BCP dot-array-based moiré superstructures. (a) Formation of a bottom layer of hexagonal dots *via* self-assembly of a BCP, followed by solvent annealing and reactive ion etching (RIE) to transform the BCP into a hexagonal lattice of silica dots. (b) Deposition of a top layer BCP film on the preformed nanopattern of silica dots from (a). (c) Annealing of top layer BCP films results in orientational alignment of the top layer BCP dot array. (d) RIE of the top layer converts the BCP to silica dots, resulting in a moiré superstructure.

Table 1. Pitch, Dot Diameter, and Height of Silica Nanodot Arrays Converted from the Annealed BCPs/BCP Blend Used in This Study^a

abbreviation	composition	pitch (nm)/HIM	diameter (nm)/SEM	height (nm)/AFM
P22	PS- <i>b</i> -PDMS (22.5K–4.5K)	23.4(5)	12.0(1.6)	2.9(4)
P43	PS- <i>b</i> -PDMS (43K–8.5K)	34.1(6)	15.9(7)	5.0(4)
B30	PS- <i>b</i> -PDMS (31.5K–14.5K) + 30 wt % PS (10K)	42.5(5)	21.8(8)	7.3(5)

^aSEM, HIM, and AFM refer to scanning electron microscopy, helium ion microscopy, and atomic force microscopy, respectively.

respectively, and the dot diameter, pitch, and height of each silica dot array are listed in Table 1. The layered structures are denoted by their deposition sequence. For example, P22-(bottom) + P43(top) is a sample where P22 is used as the bottom layer and P43 used as the top layer. The layered structures produced in this work are P22(bottom) + P43(top), P43(bottom) + P22(top), P43(bottom) + B30(top), and B30(bottom) + P43(top).

Examples of three moiré superstructures on flat silicon substrates, resulting from combinations of the BCPs listed in Table 1, are shown in Figure 2. Figure 2a, c, and e show SEM micrographs of the three moiré superstructures, and Figure 2b, d, and f are schematic illustrations indicating the relative rotation of the individual dot arrays in the three moiré superstructures. Figure 2a and c utilize the same pair of BCPs,

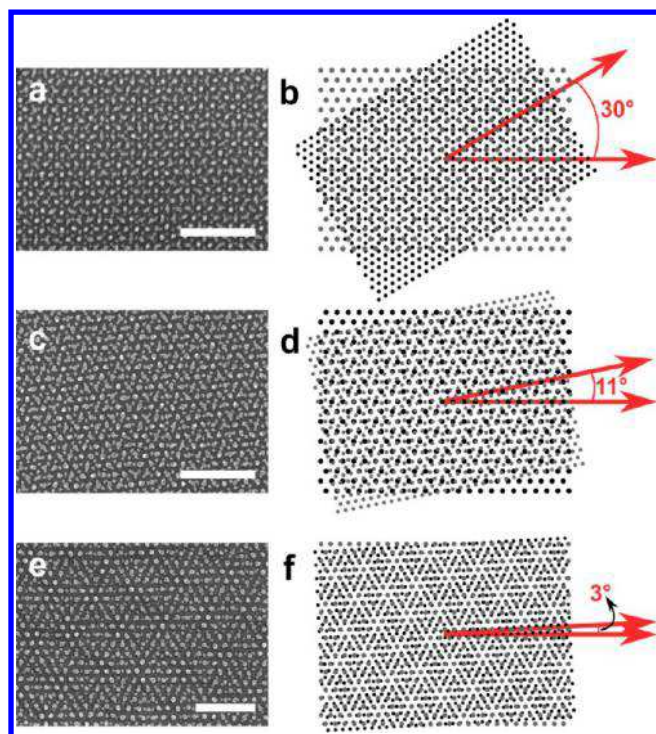


Figure 2. Left column: SEM micrographs of moiré superstructures formed from sequential annealing of two incommensurate BCP combinations. Right column: corresponding schematic representation. (a, b) P22(bottom) + P43(top). (c, d) P43(bottom) + P22(top). (e, f) P43(bottom) + B30(top). In (b), (d), and (f), the bottom layers are portrayed in black, and the top layers in gray. All scale bars are 250 nm.

but in reverse order, and Figure 2e examines a higher molecular weight BCP and a BCP/homopolymer blend. In Figure 2a the BCP with the lower molecular weight, P22 (PS-*b*-PDMS (22.5K–4.5K)), was applied as the bottom layer of dots, having a pitch of ~ 23 – 24 nm (Table 1). The top layer of dots was formed from a higher molecular weight BCP, P43 (PS-*b*-PDMS (43K–8.5K)), which consequently has a larger pitch of ~ 34 nm (Table 1). The resulting majority phase is shown in Figure 2a (vide infra for discussion of determination of majority phase). The relative rotation angle between the first and second layers is 30° . When carried out in the reverse order, with the bottom dot pattern formed from P43 formed, followed by P22 as the top layer, a different moiré superstructure is observed (majority phase, Figure 2c). The relative rotation angle between the two layers in this case is about 11° . Starting with P43 (pitch of ~ 34 nm) as the bottom dot pattern, B30, which has a pitch of ~ 42 – 43 nm (Table 1), was used to form the top layer of dots; the majority phase of the resulting moiré superstructure is shown in Figure 2e. In the latter case, the relative rotation angle between the two layers is near 3° .

Figure 3 shows a representation of the individual layers in the three distinct majority phase moiré superstructures, as observed by SEM, in Figure 3a–c. The dots in Figure 3d–i were manually separated based on the differences in dot sizes between the two layers; the sizes of the dots are displayed as the average size of the corresponding BCP pattern determined from the SEM micrograph. The bottom layer dot nanopatterns, Figure 3d–f, display long-range hexagonal ordering within the 850 nm \times 850 nm area of the micrograph. The top layers, Figure 3g–i, also show long-range hexagonal ordering despite

undergoing self-assembly on a surface with protruding silica dots of a different spacing. Figure 3j–l correspond to the original SEM micrographs in Figure 3a–c, with the layers stacked according to the annealing sequence: blue dots comprise the bottom layer and red dots the top layer. Random sampling *via* high-magnification SEM generally revealed a consistent moiré superstructure (majority phase) across the substrate. From these observations it was hypothesized that a unique set of preferential orientation relationship(s) exists between any two BCP dot arrays. However, from these micrographs it was also observed that there was some variance in the relative orientation of the lattices, as well as a sparse amount of other configurations.

In order to test the hypothesis of preferential lattice orientations, it was necessary to perform high-resolution large-area imaging of multiple films (made under identical processing conditions) in order to quantify the distributions of relative rotation between the two lattices, yielding statistically meaningful results. Helium ion microscopy (HIM) was used to acquire the high-resolution (8192×8192 pixels) large-scale micrographs [$20 \mu\text{m} \times 20 \mu\text{m}$ for P43(bottom) + B30(top), $15 \mu\text{m} \times 15 \mu\text{m}$ for P22(bottom) + P43(top) and P43(bottom) + P22(top)]. From these micrographs, dot positions of the two layers in the moiré superstructures were separated using fast Fourier transform (FFT) filtering of the HIM images (see Methods section), and the orientations of each individual layer were calculated at each dot position using the data processing analyses, described in the Methods section. The relative orientations of the top and bottom layers were then calculated by taking the difference of these angles. Since the relative rotation angles are calculated per dot, those angles can be color mapped and plotted on the dot positions to form an image over the entire micrograph to reveal preferred domains, as well as other distinct superstructures. Examples of these processed images are shown in Figure 4, along with labeled details of these high-magnification images (Figure 4b–e and g–j) to reveal the nature of the moiré superstructures. Figure 4a and f are processed HIM micrographs of P43(bottom) + P22(top) and P43(bottom) + B30(top), respectively. As the hexagonal dot pattern has 6-fold circular symmetry, the relative rotation angle has been mapped on a cyclical color scale with a range of -30° to $+30^\circ$. As can be seen upon close inspection of Figure 4, the areas that have the same relative rotation, represented by the same colors, correspond to areas with the same patterns. These patterns have the same structure and relative rotation between the layers, although they do not have the same absolute rotation. It can be seen that these data are evidence of a preferential orientational relationship between the two layers.

Shown in Figure 5 are spatial mappings of the lattice orientations for different bottom layers (a–c) and corresponding top layers (d–f). From these lattice orientation maps of the bottom and top layers, the relative rotation maps are calculated and shown in Figure 5g–i. The maps portray a $15 \mu\text{m} \times 15 \mu\text{m}$ area of P22(bottom) + P43(top) and P43(bottom) + P22(top) and a $20 \mu\text{m} \times 20 \mu\text{m}$ area of P43(bottom) + B30(top). The lattice angles are measured as described in the Methods section from the horizontal axis of the image, where a color represents the lattice orientation as indicated by the cyclical color map, with a range of -30° to 30° . From these maps, the BCP dot pattern grains, grain orientations, and their associated grain boundaries are easily differentiated.

The relative rotation map for P43(bottom) + P22(top), shown in Figure 5h, indicates the presence of two phases with

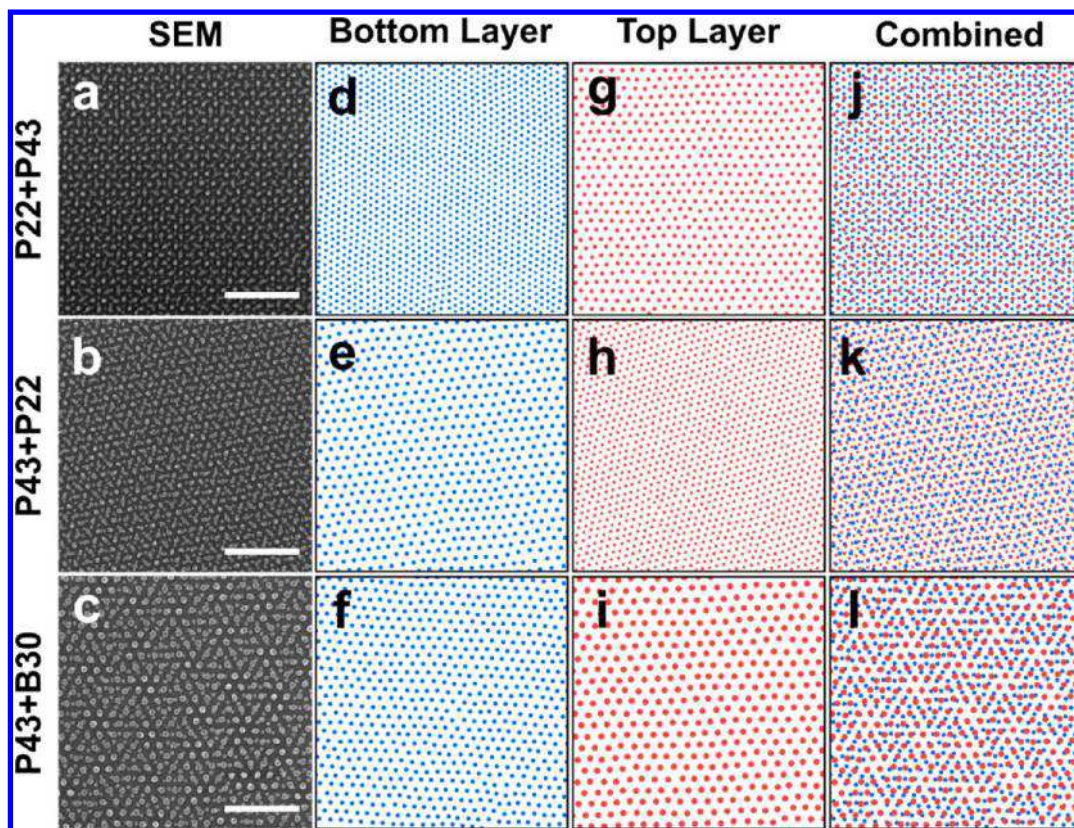


Figure 3. Separation of BCP moiré superstructures into top and bottom layers. (a–c) SEM micrographs, (d–f) dot patterns of the bottom layer, (g–i) dot patterns of the top layer, (j–l) combined bottom and top layers of the three moiré superstructures. All scale bars are 250 nm.

preferential rotation angles of -10 and $+10$ degrees. These patterns share the same moiré structure but have opposite chirality, as seen in the detailed dot patterns found in Figure 4c and g. Every preferential relative rotation angle at angles other than 0° or 30° will exhibit a selection between two degenerate lattice orientations, resulting in left- and right-handed domains of the same moiré structure, which on the chosen scale are seen as positive and negative angles of equal magnitude.⁴⁵ To clearly show the preferential relative rotation angles/lowest energy configuration of each sample, the absolute values of the relative rotation angles were plotted in Figure 5j–l. After accounting for the left- and right-handed domains, only the blue color, corresponding to an angle of about 10° , appears in the absolute relative rotation angle map in Figure 5k, revealing that the pattern has only one preferential dot configuration/moiré superstructure. Upon close inspection, all three samples show a preferred relative rotation angle and, thus, a preferred moiré superstructure. The preferential relative rotation angle between the two BCP layers of P22(bottom) + P43(top) is about 30° (Figure 5g and j). The relative rotation angle map and the absolute relative rotation map of P43(bottom) + B30(top) show a preferential relative rotation angle around 0° .

Inspection of the individual layers in Figure 5a–f shows that the grains of the top layer generally align with the bottom layer. However, as seen in the relative rotation maps (Figure 5g–i), the overlap of the grains is not perfect, as there are thin regions with very different relative lattice orientations. It is these grain boundary transition regions between the top and bottom layers that account for the different moiré superstructures occasionally observed in SEM (see Figure S3).

A moiré superstructure is uniquely defined by a pitch ratio (defined as the ratio of the dot pitch of the top layer divided by that of the bottom layer) and a relative rotation between the layers. As such, in order to analyze the moiré structures found in these samples, the distributions of these quantities are shown in Figure 6, which are calculated using a 2D and 1D kernel density estimation (KDE).⁷² Each chart is an ensemble of statistics from multiple HIM micrographs and samples, with the total number of dots indicated in the KDE as N . The median pitch ratios and relative rotation angles of five different configurations of sequentially deposited BCP bilayers are summarized in Table 2. The native pitch ratio is also listed, which is defined as the ratio of dot spacings found in the corresponding single (or bottom) layer patterns. The dot pitch distributions of the dot patterns from the separated layers can be seen in Figure S4. Two additional configurations are listed in the table, B30(bottom) + P43(top) and B30_{oc}(bottom) + P43(top), which will be discussed later.

Several observations can be made from these KDEs. First, for any given configuration, it is seen that all relative rotations are clustered around an angle of θ_0 and $-\theta_0$ (which corresponds to the chiral but degenerate moiré superstructure), with standard deviations on the order of $\sim 3.5^\circ$. These data substantiate the hypothesis that preferred moiré superstructure(s) can be formed for a given pair of incommensurate BCP lattices, further suggesting that these moiré superstructures represent a minima in the energy landscape of these incommensurate BCP lattices. Inspection of Table 2 reveals that differences in native and measured pitch ratio are between 0 and 2%. These data imply that the registration force from the bottom layer is insufficiently strong to induce a large global strain of the top

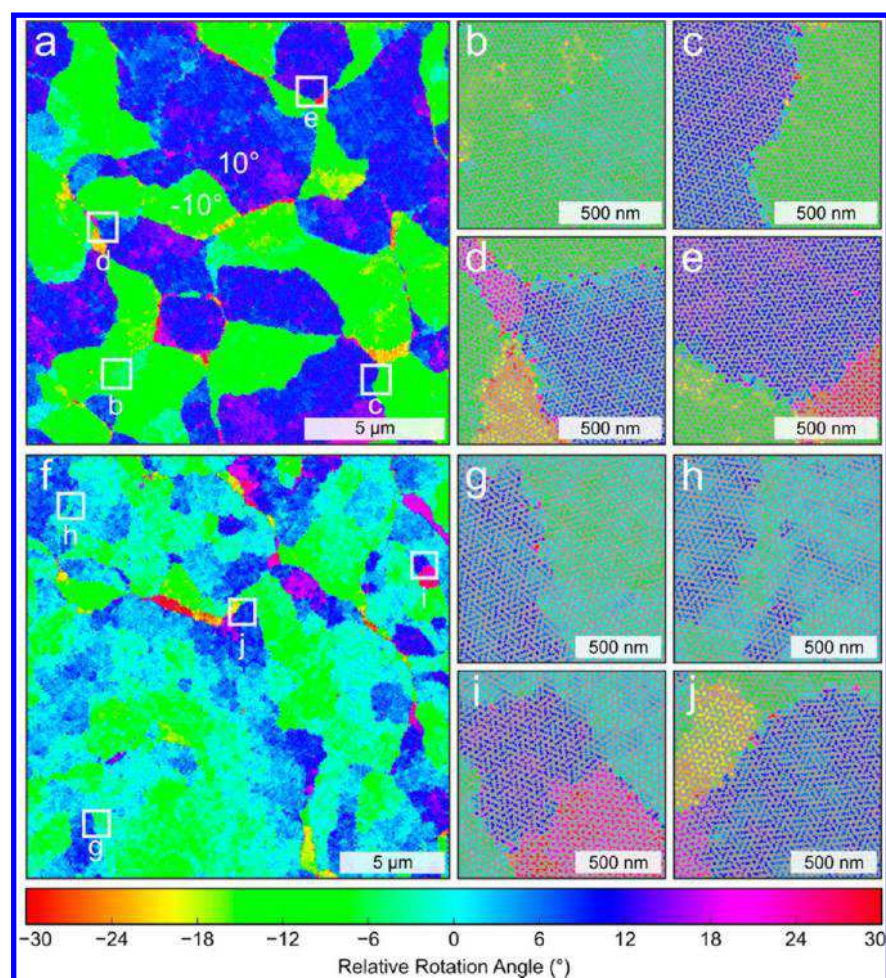


Figure 4. Large-area high-magnification map of relative lattice orientation between top and bottom BCP dot arrays. (a) Relative rotation angles of the bottom and top dot layers, derived from P43(bottom) + P22(top), as defined as the angular difference between the lattice orientation of the two dot patterns. In this map, a single color corresponds to a particular moiré superstructure. (b–e) Higher magnification of (a) as labeled. (f) Dot lattice relative rotation angles in the combination of P43(bottom) + B30(top). (g–j) Higher magnification of (f) as labeled.

layer lattice spacing. Lastly, the 2D KDEs show little correlation between the measured pitch ratio and the relative rotation, seen by the on-axis orientation of the elliptical peak shape and the near-zero Pearson product-moment correlation coefficients found in Table 2. This result suggests that local variations in relative lattice orientation do not significantly modify the local pitch ratio.

In addition to the previous three BCP combinations, B30(bottom) + P43(top) was also produced. However, the resulting pattern formed by this combination, shown in Figure 7a–d, Figure S5a–d, and Figure S6a–d, differs significantly. In contrast to the other three examples analyzed, the spherical micelle domains of the top layer, P43, tend to deviate from their equilibrium lattice positions, having a higher density of point defects, which can be clearly seen *via* the dot separation in Figure 7b. Interestingly, despite the higher defect density in the top layer of P43, there is still a preferential orientational relationship between the top and bottom layers. As seen in Figure 7d, the distribution of relative rotation angles is consistently centered around 0° , although quite broad with respect to both pitch and angle. The relative rotation is fit with two peaks at angles of $\pm 2.6(5.0)^\circ$. Two peaks were used because the resulting pattern has areas that twist from $\sim 0^\circ$ to $\sim +5^\circ$ and others that twist from $\sim 0^\circ$ to $\sim -5^\circ$, as can be clearly

seen in Figure 7c, where there are distinct regions of green and blue, as opposed to a uniform mixture of the two colors. The different registration observed in this system may be due to the size of the silica dots derived from the B30 BCP blend, which produces dots with a height of 7.3 nm and a rather large diameter of 21.8 nm compared to the dots derived from P43, which have a height of 5 nm and a diameter of 15.9 nm.

To further study the effects of bottom layer dot size on the epitaxy of the top layer, the first layer of the B30 silica dots was etched by RIE with an extra 5 s of CF_4 (100 mT, 50 W) to reduce the dot size to 5.2 nm in height and 18.2 nm in diameter (Figure S7). This configuration is defined as B30_{oe}(bottom) + P43(top). Figure 7e–h shows the resulting pattern and analysis of the registration of the top layer formed from P43 on B30_{oe}. The epitaxial registration of the top layer on B30_{oe} is remarkably different when compared to the previous B30(bottom) + P43(top) sample. One of the most striking differences is the dramatic increase of long-range ordering observed in the top layer (compare Figure 7b and f). Second, the distribution of the relative rotation angles between the top and bottom layers has two clearly defined peaks centered at $+5^\circ$ and -5° (Figure 7d and h). Moreover, the relative rotation map of B30_{oe}(bottom) + P43(top) (Figure 7g) appears to be much more similar to the other BCP combinations used in this work

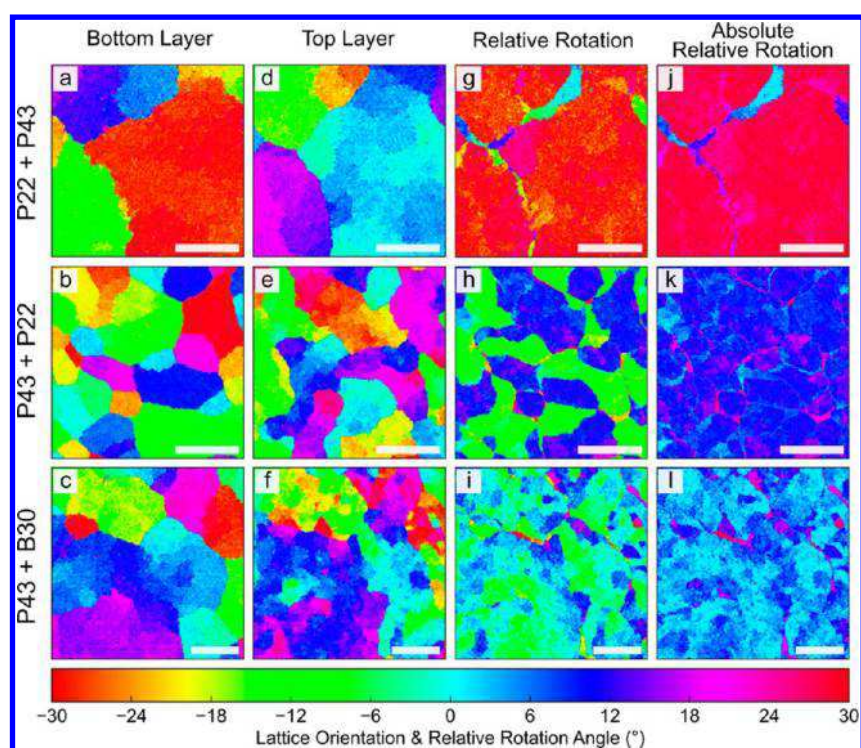


Figure 5. Grain structures of top and bottom layers and corresponding relative orientations between layers. (a–f) Bottom and top layer dot-pattern lattice orientations (relative to the horizontal axis of the image). (g–i) Relative rotation angle between dot patterns of the first and second layers as described in Figure 4. (j–l) Absolute values of previous relative rotation angles showing the chiral symmetry resulting from the degenerate lattice orientations in the double-layer patterns. All scale bars are 5 μm in length. Interactive and full-resolution images of all of these maps can be found online at http://maverick.chem.ualberta.ca/bcp_micrographs/ using the Web Deep Zoom Toolkit developed at NIST.⁷¹

(Figure 5), where there are large micrometer-sized regions possessing a single relative orientation, which are delineated by grain boundaries of either the top or bottom layer. Unlike B30(bottom) + P43(top), the 2D KDE of B30_{oc}(bottom) + P43(top) (Figure 7h) shows two well-resolved peaks. The relative rotation angle between the top P43 layer and the bottom B30_{oc} is fit to 4.8(2.9)°. The pitch ratio of B30_{oc}(bottom) + P43(top) was measured to be 0.803(17), which is very close to the native pitch ratio (Table 2). These results indicate that the pitch ratio is not the only parameter that determines that resultant structure, as the relative dot sizes can also strongly influence the final morphology. In this case, as the dot size of the bottom layer is reduced, the registration with the top layer weakens. At these smaller dot sizes, the registration is insufficient to create point defects in the top layer, but is sufficiently strong such that the configurational energy is minimized with a relative rotation of $\pm 5^\circ$. Similar observations have also been reported in a study of self-assembly of PS-*b*-PDMS cylinders over silica pillar arrays, formed *via* *e*-beam lithography of HSQ.⁷³ In that work, differences in the silica post height of as little as 3 nm, in the range of 12 to 26 nm, induced substantial changes in the morphology and orientation of the self-assembled microdomains of the PS-*b*-PDMS BCP. Similar to the observations presented in this work, the phenomenon of preferential orientation between two different hexagonal lattices has also been widely reported for the alignment of hard two-dimensional atomic materials. Specifically, graphene on hexagonal boron nitride (hBN),⁷⁴ hBN on Ir(111),⁷⁵ graphene on Ir(111),⁷⁶ and graphene on transition metal surfaces⁷⁷ show well-defined preferred orientations. These resulting configurations are found to be

reasonably well predicted by a simple two-dimensional model, where the configurational energy of all possible moiré superstructures can be estimated for any pair of infinitely large defect-free hexagonal lattices.⁷⁸ Unfortunately, this model fails to predict the majority of experimentally observed configurations for the BCP lattices investigated in this work. In order to properly predict the moiré superstructures between BCP dot lattices, a much more sophisticated model is necessary. Specifically, the three-dimensional geometrical nature of these structures is fundamentally important, which is clearly illustrated in Figure 7, where a 2 nm reduction in dot height significantly altered the observed moiré structure. Moreover, the significant deviations from ideal hexagonal positions (in all three spatial dimensions) for BCP dot arrays will play an important role in the energy minimization. As such, it is believed that simulation methods such as self-consistent field theory (SCFT) or molecular dynamics (MD) are necessary to predict and more deeply understand the formation of these BCP moiré superstructures. It is also emphasized that these simulations will have been done over a very large simulation volume to account for low-angle moiré patterns, domain size effects, and deviations from ideal positions for the bottom registration lattice.

CONCLUSIONS

Sequential self-assembly of incommensurate BCP dot arrays leads to preferred orientations, thus providing a route toward a unique set of large-area, single-grain moiré superstructures. The registration force of the bottom layer of dots is sufficiently strong to bring about registration of the top layer, resulting in formation of a majority phase. The advantages of nano-

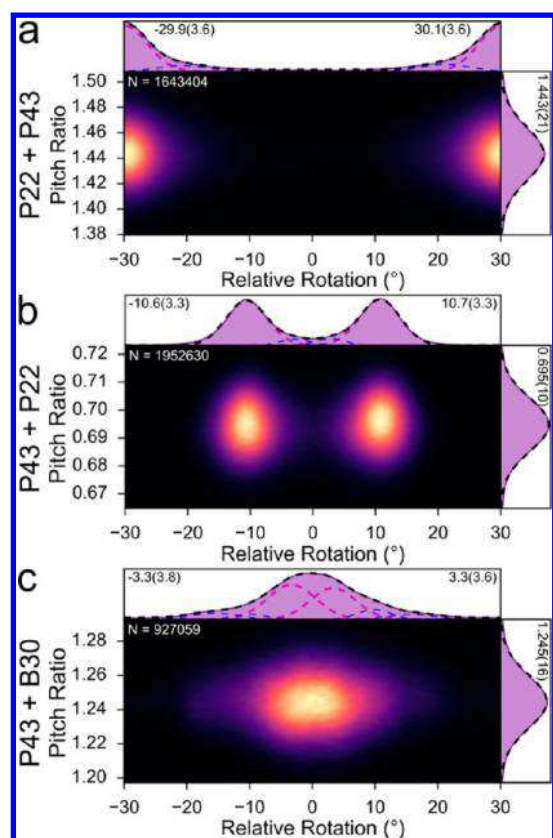


Figure 6. 2D and 1D kernel density estimations showing the distribution of pitch ratios (L_2/L_1) and relative rotation angles found in the moiré superstructures. (a) Statistical representation of P22(bottom) + P43(top) comprising 8 HIM micrographs ($15 \mu\text{m} \times 15 \mu\text{m}$) from three different samples, sampling a total of over 1.6 million dots. (b) Statistical representation of P43(bottom) + P22(top) comprising 10 HIM micrographs ($15 \mu\text{m} \times 15 \mu\text{m}$) from three different samples, sampling a total of over 1.9 million dots. (c) Statistical representation of P43(bottom) + B30(top) comprising 5 HIM micrographs ($20 \mu\text{m} \times 20 \mu\text{m}$) from one sample, containing over 0.9 million dots.

Table 2. Native Pitch Ratios Calculated from Bottom Layer HIM Data, Pitch Ratios (L_2/L_1), Relative Rotation Angles, and the Correlation Coefficients between the Pitch Ratio and Absolute Relative Rotation Angle for the Resulting Moiré Superstructures^a

BCP layers (bottom + top)	native pitch ratio (L_2/L_1)	measured pitch ratio (L_2/L_1)	relative rotation (deg)	correlation coefficient
P22 + P43	1.46(4)	1.443(21)	29.9(3.6)	0.007
P43 + P22	0.687(19)	0.695(10)	10.7(3.3)	0.018
P43 + B30	1.245(27)	1.245(16)	3.3(3.8)	0.045
B30 + P43	0.803(17)	0.813(19)	2.6(5.0)	-0.004
B30 _{oe} + P43	0.803(17)	0.789(9)	4.8(2.9)	-0.007

^aB30_{oe} refers to a B30 sample that was overetched by RIE to decrease dot size. The listed uncertainties are the measured standard deviations of each quantity.

lithography *via* self-assembly of BCPs are multifold and include the low cost of processing, their high resolution, and well-developed methods to transfer the BCP nanopattern to the underlying substrate. This class of registration between BCP layers suggests an avenue to access a complex family of patterns and motifs, through an entirely bottom-up process. As is always

the case with nanopatterning *via* self-assembly of BCPs, subtle effects are important, including the critical role of dot size, grain boundaries between dot domains, and the annealing process. Further investigation into the fundamental aspects of self-assembly of the second layer during the annealing step, coupled with large-scale statistical analysis of the resulting patterns, will lead to a better understanding of registration and, hence, reduce the level of defects in the resulting nanopatterns.

METHODS

Materials. All BCPs (PS-*b*-PDMS (31K-14.5K), PDI 1.15; PS-*b*-PDMS (43K-8.5K), PDI 1.04; PS-*b*-PDMS (22.5K-4.5K), PDI 1.09) and polystyrene (PS) (10K, PDI 1.09) were obtained from Polymer Source Inc. Toluene and tetrahydrofuran (THF) were purchased from Fisher Scientific. Silicon wafers (<100>, 4 in. diameter, thickness $525 \pm 25 \mu\text{m}$, p-type (boron doped), resistivity $< 0.005 \Omega\text{-cm}$) were purchased from WRS Materials. Sulfuric acid (96%) and hydrogen peroxide (30%) were purchased from Avantor Performance Materials.

Silicon Wafer Dicing and Cleaning. Silicon wafers were diced into $1 \text{ cm} \times 1 \text{ cm}$ squares by a DSA 321 dicing saw and cleaned with piranha solution [3:1 v/v sulfuric acid (96%)/hydrogen peroxide (30%)].

Imaging. All images were taken with a Hitachi S4800 scanning electron microscope (15 kV, 20 μA), a Zeiss scanning helium ion beam microscope (30.8 kV, 10 μm aperture, spot size 4), or atomic force microscope (Digital Instruments/Veeco, tapping mode under ambient condition).

BCP Thin-Film Self-Assembly and Reactive Ion Etching. The general experimental procedure used in this work of sequential annealing of block copolymer thin films and conversion into silica dot patterns is shown in Figure 1. A detailed description of BCP thin-film preparation, annealing procedure, annealing conditions, etching recipes for each BCP sample, and sequential annealing procedures can be found in previous papers.^{68,79} Briefly, the fabrication process begins by spin-casting a dot-forming BCP or BCP/PS blend thin film (bottom layer) on piranha-cleaned $1 \text{ cm} \times 1 \text{ cm}$ silicon chips from a 1 wt % toluene solution. For each BCP or BCP/PS blend, the film thickness was optimized to form a single-layer dot pattern after solvent annealing. In this paper, three different BCPs and a BCP/PS blend were used, PS-*b*-PDMS (13K-14.5K)/30 wt % PS (denoted as B30), PS-*b*-PDMS (43K-8.5K) (denoted as P43), and PS-*b*-PDMS (22.5K-4.5K) (denoted as P22). The optimized film thicknesses for B30, P43, and P22 were ~ 32 , ~ 30 , and $\sim 25 \text{ nm}$, respectively. The BCP or BCP/PS blended films were annealed in a custom-made solvent annealing chamber, where THF was used as the annealing solvent.^{68,79} Film thickness was monitored in situ during the annealing process using ellipsometry ($\lambda = 632.8 \text{ nm}$, $\theta = 70^\circ$). The optimized final swelling degrees (swollen film thickness/initial film thickness) of each sample were ~ 2.0 for B30 and P43 and ~ 1.6 for P22. After annealing, hexagonally packed spherical PDMS domains were bound within the PS matrix. The annealed BCP or BCP/PS blend films were then converted to a silica dot array by applying a CF_4/O_2 RIE treatment (Figure 1a). The etching recipe for each BCP film can also be found in our previous paper.⁶⁸ During RIE etching, the PDMS domains are oxidized to SiO_2 and PS domains are etched away. Following the first patterning step, the top layer of the BCP or BCP/PS blend thin film was then spin-cast onto the now-patterned silicon substrate (Figure 1b). The top layer of the BCP film was annealed and converted to silica dots using identical annealing and RIE conditions as those of the bottom layer.

Data Processing. Statistical analyses of lattice angles and dot pitch were taken from a collection of HIM micrographs with a 15 or $20 \mu\text{m}$ field of view and a resolution of 8192×8192 pixels (1.8 or $2.4 \text{ nm}/\text{pixel}$, respectively). The statistical analysis of P22(bottom) + P43(top) was carried out using eight HIM micrographs ($15 \mu\text{m} \times 15 \mu\text{m}$) from three different samples comprising over 1.6 million dots. P43(bottom) + P22(top) statistics were collected from 10 HIM micrographs ($15 \mu\text{m} \times 15 \mu\text{m}$) from three different samples comprising over 1.9 million dots. P43(bottom) + B30(top) statistics were collected from five HIM

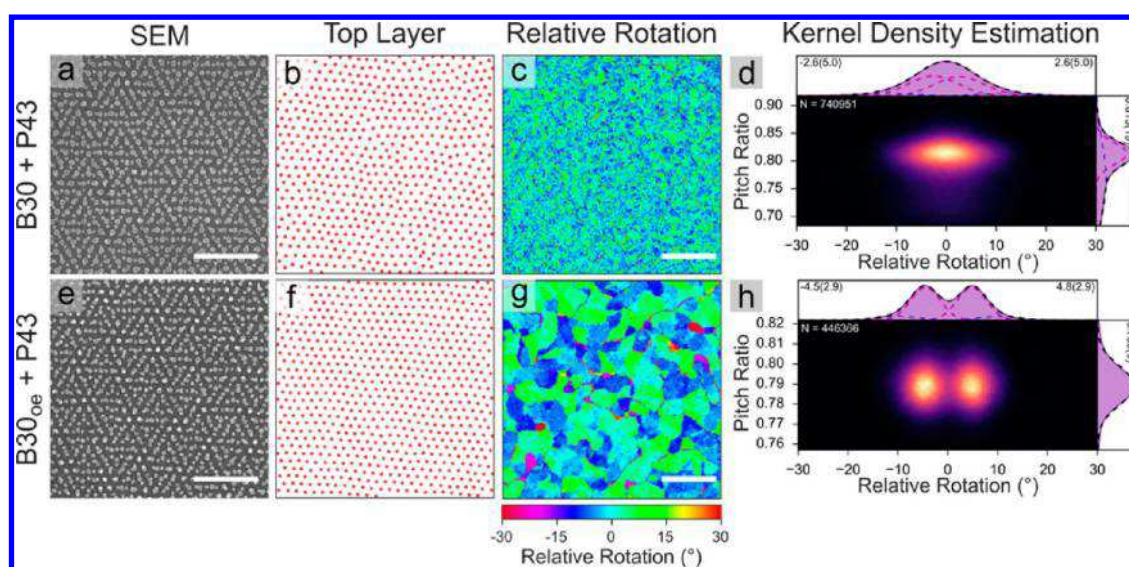


Figure 7. Effect of bottom layer dot size on the resulting moiré superstructures. (a–d) Data for the B30(bottom) + P43(top) BCP moiré superstructures. (e–h) Data for a B30_{oe}(bottom) + P43(top) moiré superstructures where the bottom B30 BCP layer was etched by RIE for an extra 5 s, resulting in the formation of smaller silica dots. Scale bars in SEM micrographs (a, b, e, and f) are 250 nm, and scale bars in the relative rotation angle maps (c and g) are 5 μm in length.

micrographs ($20\ \mu\text{m} \times 20\ \mu\text{m}$) from one sample comprising over 0.9 million dots. P43(bottom) + B30(top) statistics were collected from four HIM micrographs ($20\ \mu\text{m} \times 20\ \mu\text{m}$) from one sample comprising over 0.7 million dots. The dot positions corresponding to the top and bottom BCP layers were separated *via* Fourier filtering using Gwyddion analysis software.⁸⁰ Specifically, due to the differences in dot pitch (L_0) of each layer, the dots from a single layer (either top or bottom) can be revealed by application of a bandpass filter centered on the fundamental frequency of each lattice ($k \approx 2/\sqrt{3}L_0^{-1}$). Dot positions were then determined by a thresholding algorithm (Ostu's method). It is noted that this type of separation is possible only on patterns that do not have overlapping fundamental frequencies.

To measure the pitch and angle of each dot, the positions of the six nearest neighbors of each dot were first determined. The pitch of each dot was then taken as the mean distance between the central dot and its six nearest neighbors. The lattice angle of each dot was defined as the orientation of the corresponding coordination shell of each dot, relative to the horizontal axis of the image; this was determined by calculating the angle between the central dot and each of its coordinating dots (modulo 60°). The circular mean of these six angles was then used to calculate the lattice orientation.

ASSOCIATED CONTENT

Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acsnano.7b00322.

SEM and AFM micrographs of single-layer BCP dot arrays, SEM characterization and analysis of grain boundaries between moiré superstructures, distributions of dot pitches for top and bottom layers, analysis of moiré structures with an overetched bottom layer, and distributions of dot height (PDF)

AUTHOR INFORMATION

Corresponding Authors

*E-mail: eluber@ualberta.ca.

*E-mail: jhuriak@ualberta.ca.

ORCID

Jillian M. Buriak: 0000-0002-9567-4328

Notes

The authors declare no competing financial interest.

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